

KABARAK UNIVERSITY

(ELAND COLLEGE)

UNIVERSITY EXAMINATIONS

BRIDGING CERTIFICATE COURSE IN MATHEMATICS

AUGUST 2008 EXAMINATIONS

COURSE CODE: BMATH/003/011

COURSE TITLE: BASIC CALCULUS

STREAM: BRIDGING

DAY: WEDNESDAY

DATE: 27TH AUGUST 2008

TIME: 9.00 AM TO 11.00 AM

INSTRUCTIONS TO CANDIDATES

Attempt question ONE and any other TWO questions.

Question ONE (30mks)

a) Given that $h(x) = x^2 - x$, find the values of:

i) $h(10)$

ii) $h(-3)$

iii) $h\left(\frac{1}{2}\right)$

iv) $h(t + 1)$ (6mks)

b) If $f(x) = x^3 + 4x^2 - 12x$ and $g(x) = x - 2$, find $\frac{f(x)}{g(x)}$ (2mks)

c) Calculate $\frac{x^2 - 25}{x - 5}$ (3mks)

d) Use the first principle to find $\frac{dy}{dx}$ when $y = x^2 - 4x$. (3mks)

e) Calculate $\frac{dy}{dx}$ in the following:

i) $y = 3x^2 - 2x + 5$ (2mks)

ii) $y = 2x(1 - x^2)$ (2mks)

iii) $y = \frac{x^2 + 4}{x - 3}$ (3mks)

f) Evaluate the following integrals:

i) $\int (x^2 + 6x - 4) dx$ (2mks)

ii) $\int_1^2 (5x - x^2) dx$ (3mks)

g) Find the equation of the tangent to the curve.

$Y = 2x^3 - x^2 + 4x - 1$ at $x = -2$ (4mks)

Question 2 (20mks)

a) If $f(x) = ax + \frac{b}{x}$ and if $f(2) = 9$ and $f(3) = 16$, evaluate a,b and find the values of

x for which $f(x) = 0$ (3mks)

b) Find the derivative $(\frac{dy}{dx})$ of the function $y = 2x^2 + 2$ from the first principles.

(3mks)

c) Find the value of the gradient of $y = x^4 - 3x^2 + 4x + 1$ when $x = 1$

(2mks)

d) A particle starts from rest and moves a distance of 5 metres in t seconds,

where $S = \frac{1}{6}t^3 + \frac{1}{4}t^2$. What is its acceleration when $t = 2$ (2mks)

e) The gradient of a curve at any point (x, y) is $7 - 2x$. given that the curve passes through (3,2), Find:

i) the equation of the curve.(4mks)

ii) the points where the curve crosses the x-axis. (4mks)

iii) The point where the gradient is zero. (2mks)

Question 3 (20mks)

a) Find the equations of the tangent and normal to the curve.

$$y = x^3 - 2x^2 - 2x - 3 \text{ at } x = 2 \quad (10\text{mks})$$

b) A particle moves in a straight line and its distance is 5 metres from a point given by:

$$S = 45t + 11t^2 - t^3$$

- i) find an expression for the velocity v in terms of t
- ii) find an expression for the acceleration in terms of t
- iii) find both the velocity and acceleration when $t = 3$ seconds.
- iv) prove that the particle will come to rest after 9 seconds.

(10mks)

Question 4 (20mks)

a) Find $\frac{dy}{dx}$ given that:

i) $y = \frac{x^2}{x+1}$ (2mks)

ii) $y = (x^2 + 2)(x^3 - 3)$ (2mks)

b) Use the second derivative to determine whether the function has a minimum or maximum. $y = x^3 - 6x^2 + 9x + 2$ (3mks)

c) Calculate the area between the curve $y = 3x - x^2$ and the x-axis from the point $x = 0$ to $x = 5$. (5mks)

d) Simplify $\frac{x^7 + 4x^3 - 3x}{x^2 + 2x}$ (3mks)

e) Find the equation of a line, perpendicular to the line $2y = 3x - 5$ and passing through $(2, 7)$ leaving your answer in the form $ax + by + c = 0$ where a, b, c are constants. (3mks)

f) The domain of the function $f(x)$ is $\{1, 2, 3, 4, 5\}$. Find the range if

$$f(x) = 5x^2 + 3 \quad (2\text{mks})$$

Question 5 (20mks)

a) Arrange the equation $3x + y + 6 = 0$ in the form $y = mx + c$, hence write down the gradient and y-intercept. (3mks)

b) Given that $f(x) = 10x$ and $g(x) = x + 3$ find $fg(x)$ and hence the value of $fg(2)$ (3mks)

c) i) Use the trapezium rule to find the area between the curve $y = x^2 + 4$, the x-axis and the co-ordinates $x = 0$ and $x = 4$. Take values of x at intervals of $\frac{1}{2}$ units. (5mks)

ii) Use integration to find the exact area in c) (i) above. (3mks)

d) The gradient function of a curve is given by

$$\frac{dy}{dx} = 3x^2 - 8x + 2. \text{ If the curve passes through point } (0, 2), \text{ find its equation.}$$

(4mks)

e) Find the equation of the tangent to the curve. $y = x^2$ at the point $(5, 25)$

(2mks)