

**KABARAK**



**UNIVERSITY**

**UNIVERSITY EXAMINATIONS**

**2009/2010 ACADEMIC YEAR**

**FOR THE CERTIFICATE OF PRE- UNIVERSITY BIOLOGY**

**COURSE CODE: PMATH 022**

**COURSE TITLE: BASIC CALCULUS**

**STREAM: PRE – S2**

**DAY: THURSDAY**

**TIME: 2.00 – 4.00 P.M.**

**DATE: 03/12/2009**

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**INSTRUCTIONS:**

Attempt **Question One** and **any other two** questions.

**PLEASE TURN OVER**

### **QUESTION ONE (30 MARKS)**

- a) Using the first principle method, differentiate the following functions:
- i)  $y=3x+7$  (3 mks)
  - ii)  $y=15$  (3 mks)
- b) Suppose that  $f$  is a function for all real numbers  $t$  defined by:  
 $f(t)=3(2t-1)+2$ ;  
Evaluate: i)  $f(x+1)$  (2 mks)  
ii)  $fff(1)$  (2 mks)
- c) Given  $f(x)=x^3-3x^2-4x$  and  $g(x)=x-1$ , find:
- i)  $f(x)g(x)$  (2 mks)
  - ii)  $\frac{f(x)}{g(x)}$  (3 mks)
- d) Given the equation of a line  $L_1$  is  $3y+6x+10=0$ , find the equation of the line perpendicular to  $L_1$  passing through point  $(2,6)$ . (3 mks)
- e) Evaluate the following limits:
- i)  $\lim_{x \rightarrow 2} \frac{x^2 - 7x + 10}{x - 2}$  (3 mks)
  - ii)  $\lim_{x \rightarrow 3} \frac{x^2 - 9}{x - 3}$  (3 mks)
- f) Given  $f(x) = \sqrt{x}$  and  $g(x) = x + 2$ , find:
- i)  $f \circ g$  (2 mks)
  - ii)  $g \circ f$  (2 mks)
  - iii)  $f \circ f$  (2 mks)

### **QUESTION TWO (20 MARKS)**

- a) A closed tin in the shape of a cylinder is to have a capacity of  $250\pi$ mls. If the area of the metal used is to be a minimum, what should the radius of the tin be? (6 mks)
- b) Find the area enclosed by the curve  $y=x^2+5x+6$ . (4 mks)
- c) Determine whether the points  $A(1, -1)$ ,  $B(3,2)$  and  $C(8,10)$  are collinear, that is, lie on the same line. (3 mks)
- d) Differentiate
- i)  $y=2x^2+4x+15$  (2 mks)
  - ii)  $x = \sqrt{y} + 19$  (2 mks)
  - iii)  $f(x) = \sqrt{x^2 + 2x + 6}$  (3 mks)

### **QUESTION THREE (20 MARKS)**

- a) What do you understand by the following terms:
- i) continuous function (2 mks)
  - ii) "hole" (2 mks)
  - iii) limit of a function (2 mks)

b) Describe the following function:

$$f(x) = \begin{cases} x^3 + 2 & \text{if } x < 2 \\ x^2 + 6 & \text{if } x > 2 \\ 10 & \text{if } x = 2 \\ \frac{1}{x^2 - 2} & \text{if } x < 2 \end{cases} \quad (3 \text{ mks})$$

c) Differentiate and hence find the gradient at a specific point indicated.

i)  $y = (2x^2 + x + 1)(x^2 + 2)$  at (0,1) (4 mks)

ii)  $y = (3x^2 + 4)^{10}(x + 4)$  at (0,16) (4 mks)

iii)  $y = \frac{\sqrt{x^2 + 6x + 1}}{x + 1}$  at (1, -3) (3 mks)

#### **QUESTION FOUR (20 MARKS)**

a) Find the tangent and normal line to the curve  $f(x) = 2x^3 + 2x + 4$  at a point (1,2)

(5 mks)

b) An object moves along a line in such a way that its position at time  $t$  is  $S(t) = t^3 - 6t^2 + 9t + 5$

i. Find the acceleration and velocity statement and hence evaluate acceleration and velocity at time  $t = 2$  seconds. (4 mks)

ii. When is the object stationary? (3 mks)

c) Given  $y = 2x^2 - 6x$ ,

i. Find the critical points. (2 mks)

ii. Using the second derivative method, find the local extrema. (3 mks)

d)  $\int_{-1}^3 (3x^2 + x + 1)dx$  (3 mks)

#### **QUESTION FIVE (20 MARKS)**

a) Define a function and give an illustration of function operating like a machine.

(3 mks)

b) Using the definition of a limit, show that:

i)  $\lim_{x \rightarrow 10} (3x + 5) = 35$  (4 mks)

ii)  $\lim_{x \rightarrow 0} x^9 = 0$  (4 mks)

c) Differentiate:

i)  $y = (3x - 1)(x^2 - 4)$  (3 mks)

ii)  $y = \frac{2x + 3}{2x - 3}$  (3 mks)

d) Evaluate  $\int_{-1}^2 (x^2 + 4x)dx$  (3 mks)