



**KABARAK**

**UNIVERSITY**

**UNIVERSITY EXAMINATIONS**

**2008/2009 ACADEMIC YEAR**

**FOR THE DEGREE OF BACHELOR OF SCIENCE IN  
ECONOMICS AND MATHEMATICS**

**COURSE CODE: ECON 322**

**COURSE TITLE: ECONOMETRICS II**

**STREAM: Y4S2**

**DAY: TUESDAY**

**TIME: 2.00 – 4.00 P.M.**

**DATE: 12/8/2008**

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**INSTRUCTIONS:**

1. Answer **QUESTION ONE** and any other **TWO** questions.
2. Question **ONE** carries **30 marks** and the rest **20 marks** each.
3. Show all your workings clearly.

**PLEASE TURN OVER**

### **QUESTION ONE**

(a) Define the following terms as used in econometrics;

- (i) Identification problem **(1mk)**
- (ii) Simultaneous bias **(1mk)**
- (iii) Structural model **(1mk)**
- (iv) Recursive model. **(1mk)**
- (v) Dummy variable **(1mk)**

(b) Consider the general linear regression model;

$$Y = X\beta + \varepsilon$$

Where, Y is (n x 1) matrix  
B is (k x 1) matrix  
X is (n x k) matrix  
 $\varepsilon$  is (n x 1) matrix

- (i) Derive the ordinary least squares (OLS) estimator  $\hat{B}$  for the model. **(6mks)**
- (ii) Explain the properties of the parameter estimate in (i) above **(3mks)**

(c) A researcher wanted to analyze the effects of economic growth (Y) and inflation ( $\Pi$ ) on investment (I) using the following data;

Y	I	$\Pi$
8	6	5
11	12	2
9	10	1
6	7	3
6	3	4

- (i) Specify a regression model to be estimated **(2mks)**
- (ii) Estimate the model and interpret your results on a prior condition **(7mks)**
- (iii) Compute coefficient of determination **(3mks)**
- (iv) Conduct statistical test of the parameter estimates at 5% level of significance **(4mks)**

## **QUESTION TWO**

Given the following macroeconomic model;

$$C_t = \beta_0 + \beta_1 Y_t + \beta_2 C_{t-1} + e_1 \quad (\text{Consumption function})$$

$$I_t = \alpha_0 + \alpha_1 Y_{t-1} + \alpha_2 Y_t + e_2 \quad (\text{Investment function})$$

$$Y_t = C_t + I_t + G_t \quad (\text{definitional equation})$$

- (a) (i) Identify the predetermined and endogenous variables in the model. **(3mks)**
- (ii) Using the order and rank condition establish the identification state of consumption and investment function. **(9mks)**
- (iii) What is the appropriate estimation technique that can be used to estimate consumption and investment function? **(2mks)**

(b) Consider the following model

$$D = a_0 + a_1 P_t + \varepsilon_{1t} \quad (\text{Demand function})$$

$$S = b_0 + b_1 P_t + b_2 P_{t-1} + \varepsilon_{2t} \quad (\text{Supply function})$$

$$D = S \quad (\text{Equilibrium condition})$$

Derive the reduced form of the model. **(6mks)**

## **QUESTION THREE**

The following information was found in an economy;

Imports (M)	70	65	90	95	110	115	120	140	155	150
Income (Y)	80	100	120	140	160	180	200	220	240	260

- (a) (i) Specify a model of imports on income **(2mks)**
- (ii) Estimate the model specified in (i) as a log-log model and interpret your results. **(15mks)**

(b) Outline the effects of simultaneous equations bias in an econometric model.

**(3mks)**

## **QUESTION FOUR**

An econometrician analyzed the effects of family income (Y) and family size (N) on family household consumption expenditure (C). Using 89 households, he came up with the following information;

$$(X'X)^{-1} = \begin{bmatrix} 0.0218 & 0.0015 \\ 0.0015 & 0.0011 \end{bmatrix}, \quad (X'X) = \begin{bmatrix} 50.5 & -66.2 \\ -66.2 & 987.1 \end{bmatrix}$$

$$(X'Y) = \begin{bmatrix} 36.8 \\ 39.1 \end{bmatrix}, \quad C'C = 113.6, \quad \bar{C} = 5.8 \\ \bar{Y} = 2.9, \quad \bar{N} = 3.9$$

- (i) Specify the function to be estimated. **(2mks)**
- (ii) Calculate  $\hat{B}$ , coefficient of determination ( $R^2$ ) and variance covariance matrix. **(9mks)**
- (iii) Construct 95% confidence intervals for the partial slope coefficients. **(2mks)**
- (iv) Construct an ANOVA TABLE and test the hypothesis that  $\beta_1 = \beta_2 = 0$  at 5% level of significance. **(7mks)**

### QUESTION FIVE

The following computations in original values were obtained from data on quantity demanded (Y), its own price ( $X_1$ ) and the price of some other good ( $X_2$ );

$$n = 10 \quad \sum X_2 = 5 \quad \sum Y = 330 \\ \sum X_1 Y = 26210 \quad \sum X_2 Y = 190 \quad \sum X_1 X_2 = 456 \\ \sum X_1^2 = 64527 \quad \sum X_2^2 = 5 \quad \sum Y^2 = 11700$$

- (a) (i) Specify a regression model based on the data set above. **(1mk)**
- (ii) Estimate the model and interpret your result. **(5mks)**
- (b) Explain economic problems that one would encounter if he runs a regression using a non-stationary series. **(6mks)**
- (c) Explain in detail how Geometric lag structure can be used to reduce the number of Parameters in an econometric model so as to estimate fewer parameters. **(8mks)**