## UNIVERSITY EXAMINATIONS

# FOR THE DEGREE OF BACHELOR OF COMPUTER SCIENCE 

## COURSE CODE: PHYS 110

## COURSE TITLE: ELECTRICITY AND MAGNETISM

## STREAM:

DAY:
TIME:
2.00-4.00 P.M.

DATE:
11/08/2010

## INSTRUCTIONS:

## Instructions

- Answer Question ONE and any other TWO Questions. Question One carries 30marks while each of the other Two Questions carry 20marks.
- The following constants may be useful
- Permeability of free space $\mu_{0}=4 \pi \times 10^{-7} \mathrm{~Wb} / \mathrm{A}$
- Permittivity of free space $\varepsilon_{0}=8.85 \times 10^{-12} C^{2} / N M^{2}$
- Resistivity of Iron $\rho=9.68 \times 10^{-8} \Omega m$
- Acceleration due to gravity $g=9.8 \mathrm{~m} / \mathrm{s}^{2}$


## PLEASE TURN OVER

## QUESTION 1 ( 30 marks)

(a) i) Name two types of electric charges
ii) Explain why conductors cannot be charged by friction.
(b) i) State Coulomb's law in words and give its mathematical expression
ii) Two similar tiny balls of mass (m) are hung from silk threads of length (L) and carry equal charges (q) as shown.


Assume that $\theta$ is so small that $\tan \theta$ can be replaced by its approximate value equal to $\sin \theta$
I) To this approximation, show that for equilibrium

$$
\begin{equation*}
X=\left(\frac{q^{2} L}{2 \pi \varepsilon_{0} m g}\right)^{\frac{1}{3}} \tag{4mks}
\end{equation*}
$$

Where X is the distance between the two balls
II) If $\mathrm{L}=122 \mathrm{~cm}, \mathrm{~m}=11.2 \mathrm{~g}$ and $\mathrm{X}=4.7 \mathrm{~cm}$, what is the value of q ?
(c) A rectangular block of Iron has dimensions 1.6 cm by 1.6 cm by 25 cm . Find the conductance of the block between the two square ends.
(d) i) State Kirchhoff's current law.
ii) Determine the voltage across $\mathrm{R}_{6}$ in the given circuit
(3mks)

(f) Consider a thin ring of radius ( $\mathbf{R}$ ) carrying a uniform linear charge density ( $\boldsymbol{\lambda}$ ) around its circumference as shown

i). Derive an expression for the electric field $(\mathbf{E})$ at a point $(\mathbf{P})$ a distance $(\mathbf{X})$ from the plane of the ring along its central axis
ii). Show that if $X \gg R$, the ring become like a point charge.
(g) i) State and explain two factors that affect the magnitude of torque experienced by a current carrying wire in a magnetic field.
ii) An electron with magnetic dipole moment $3.6 \times 10^{-24} \mathrm{~J} / T$ is in a uniform magnetic field of 450 T at an angle of $30^{\circ}$. Calculate the magnetic torque on the electron.
(2mks)

## QUESTION 2 (20 marks)

(a) Define flux of a vector field and give circumstances under which flux is positive or negative.
(b) i) State Gauss' law in words.
ii) A long cylindrical solid insulator of length ( L ) and radius ( R ) has charge per unit volume ( $\rho$ ). Find the expression of electric field (E) inside and outside the cylinder and sketch the variation of $(\mathbf{E})$ against (r) for $0<\mathrm{R} \leq r$ and for $r>R$
(c) i) Define electric potential
ii) Calculate the expression for the potential energy of the system of two point charges shown


Assuming $q_{2}$ moves away from or towards $q_{1}$ along the line connecting the two charges taken to be the $X$ axis.
d) A $3.55 \mu \mathrm{~F}$ capacitor $\mathrm{C}_{1}$ is charged to a potential difference $V_{0}=6.30 \mathrm{~V}$, using a battery. The charging battery is then removed, and the capacitor is connected as shown in Figure below to an uncharged $8.95 \mu \mathrm{~F}$ capacitor $\mathrm{C}_{2}$. After the switch S is closed, charge flows from $\mathrm{C}_{1}$ to $\mathrm{C}_{2}$ until equilibrium is established, with both capacitors at the same potential difference V .

i). Calculate the common potential difference (V)
ii). What is the energy stored after the switch is closed

## QUESTION 3 (20 marks)

(a) i) What is a potentiometer?
(1mk)
ii) State two uses of potentiometers
(b) Find the equivalent resistance in the given resistor network circuit assuming that each resistor is $2 \Omega$ and hence calculate the total current in the circuit

c) Find the current in different branches in the given circuit

d) Consider a wheat-stone bridge circuit of resistors $\mathrm{R}_{1}, \mathrm{R}_{2}, \mathrm{R}_{\mathrm{X}}$ and a variable resistor $R_{S}$ connected in that order in the clockwise network loop, with a galvanometer between one diagonal and a source of e.m.f. in the other diagonal Show that at null condition,

$$
\begin{equation*}
R_{X}=R_{S}\left(\frac{R_{2}}{R_{1}}\right) \tag{3mks}
\end{equation*}
$$

e) Derive the expression of finding the electric potential difference at a point $(\mathrm{P})$ a distance $(\mathrm{Z})$ along the axis of a uniform ring of radius $(\mathrm{R})$ carrying total charge $\mathrm{Q} .(5 \mathrm{mks})$

## QUESTION 4 (20 marks)

(a) i) What is magnetic field?
(1mk)
ii) State two differences and two similarities between magnetic force and electric force.
(4mks)
(b) i) Consider a segment of conductor of length (L), cross sectional area (A), carrying current (I) placed in a uniform magnetic field $\vec{B}$, derive the expression of magnetic force $F_{B}$ experienced by the wire segment.
ii) A straight horizontal segment of copper wire carries a current $I=28 \mathrm{~A}$. What are the magnitude and direction of magnetic field needed to balance its weight? Given that it's linear mass density is $46.6 \mathrm{~g} / \mathrm{m}$.
(c) Consider a proton of charge $1.6 \times 10^{-19} \mathrm{C}$ being moved at a velocity of $3.2 \times 10^{7} \mathrm{~m} / \mathrm{s}$ in a uniform magnetic field of $1.2 \times 10^{-3} \mathrm{~T}$ at an angle of $30^{\circ}$.
i). Find the magnitude of magnetic force experienced by the proton
ii). What will be the acceleration of the proton given that its mass is $1.67 \times 10^{-27} \mathrm{Kg}$

## QUESTION 5 (20 marks)

(a) Define the following terms
i). Electromagnetic induction
ii). Magnetic flux
(b) State Lenz's law in words and give its mathematical expression
(c) i) Define inductance
ii) Calculate the inductance of a solenoid containing 400 turns if the length of the solenoid is 25 cm and its cross sectional area is $2 \mathrm{~cm}^{2}$.
(d) Consider a series RL circuit connected to a d.c. source. Derive the expression of finding energy in the circuit.
(e) An RL circuit with an inductor of inductance 8 H and resistor of $10 \Omega$ is connected to the terminals of a battery of e.m.f. 15 V and negligible internal resistance. Find
i). The initial rate of increase of current in the circuit
ii). The rate of increase at the instant when the current is 0.5 A
iii). The current 0.5 s after the circuit is closed
iv). The final steady state current

