# UNIVERSITY EXAMINATIONS <br> 2009/2010 ACADEMIC YEAR <br> FOR THE DEGREE OF BACHELOR OF SCIENCE IN 

## ECONOMICS AND MATHEMATICS

## COURSE CODE: MATH 328

COURSE TITLE: REGRESSION ANALYSIS AND ANALYSIS
OF VARIANCE

## STREAM:

DAY:
TIME:
DATE:
01/12/2009

## INSTRUCTIONS:

- Answer question ONE and any other TWO questions
- Begin each question on a separate page
- Show you workings clearly and orderly


## PLEASE TURN OVER

## QUESTION ONE (20 MARKS)

a) Define the following terms;
i) Correlation coefficient (2 marks)
ii) Rank correlation (3 marks)
iii) Regression Analysis
b) Differentiate between
i) One way ANOVA and Two way ANOVA
ii) Simple linear regression and multiple regression
c) Write the equation of the multiple regression linear model in exact linear form and stochastic form for the case of;
i) 4 independent or explanatory variables (4marks)
ii) $\quad \mathrm{k}$ independent or explanatory variables
iii) Why would you expect most observed values of Y not to fall exactly on a straight line
(2 marks)
e) The ranks of the same 15 students in two subjects $A$ and $B$ are given below; the two numbers within the brackets denoting the ranks of the same student in $A$ and $B$ respectively. $(1,10),(2,7),(3,2),(4,6),(5,4),(6,8),(7,3),(8,1),(9,11),(10,15)$, $(11,9),(12,5),(13,14),(14,12),(15,13)$. Find the rank correlation coefficient ( $\mathbf{8}$ marks)

## QUESTION TWO (20 MARKS)

The annual sales revenue (in Ksh) of a product as a function of sales force (Number of salesperson) and annual advertising expenditure (in Ksh) for the past 10 years are summarized below;

Annual sale revenue (Y) Sales force ( $X_{1}$ ) Annual Advertising expenditure ( $X_{2}$ )
$20 \quad 8 \quad 28$
$23 \quad 13 \quad 23$
$25 \quad 8 \quad 38$
$2718 \quad 16$
2123

| 29 | 16 | 28 |
| :--- | :--- | :--- |
| 22 | 10 | 23 |
| 24 | 12 | 30 |
| 27 | 14 | 26 |
| 35 | 20 | 32 |

Design a regression model to forecast the annual sales revenue of the product using matrix method.

## QUESTION THREE (20 MARKS)

Five doctors each test treatments for a certain disease and observe the number of days each patient takes to recover. The results are (recovery time in days) given below;

|  | Treatments |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Doctors | 1 | 2 | 3 | 4 | 5 |
| 1 | 10 | 14 | 23 | 18 | 20 |
| 2 | 11 | 15 | 24 | 17 | 21 |
| 3 | 9 | 12 | 20 | 16 | 19 |
| 4 | 8 | 13 | 17 | 17 | 20 |
| 5 | 12 | 15 | 19 | 15 | 22 |

Discuss the difference between doctors and treatments at 5\% level of significance.

## QUESTION FOUR (20 MARKS)

The table below gives the per capita GDP to the nearest $\$ 100(\mathrm{Y})$ and the percentage of the economy represented by Agriculture ( $X_{1}$ ) and the male literacy rate ( $X_{2}$ ) reported by World Bank Development Indicators for 1999 for 15 Latin Americans countries.

| Country | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| n | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| $Y_{i}$ | 76 | 10 | 44 | 47 | 23 | 19 | 13 | 19 | 8 | 44 | 4 | 31 | 24 | 59 | 37 |
| $X_{1}$ | 6 | 16 | 9 | 8 | 14 | 11 | 12 | 10 | 18 | 5 | 26 | 8 | 8 | 9 | 5 |
| $X_{2}$ | 97 | 92 | 85 | 96 | 91 | 83 | 93 | 81 | 74 | 93 | 67 | 92 | 94 | 97 | 93 |

(i) Find the least squares regression equation of Y on $\left(X_{1}\right)$ and $\left(X_{2}\right)$ and interpret the results
(10 Marks)
(ii) Test at the $5 \%$ level for the statistical significance of the slope parameters
(10 marks)

## QUESTION FIVE (20 MARKS)

a) For purpose of estimating this years inventory a computer company samples 6 dealers in each case getting figures for both this years and last years

Inventory last years(X) Inventory this year(Y)
$70 \quad 60$
$260 \quad 320$
$150 \quad 230$
$100 \quad 120$
20 50
60 60
i) Draw a scatter diagram for the above data (3 marks)
ii) Find the regression equation (6marks)
iii) Plot the regression line and show the deviations of actual values from the estimated values
iv) Test at the $5 \%$ level of significance for the statistical significance for the parameters
v) Find the correlation coefficient
vi) Find the coefficient of determination

