# UNIVERSITY EXAMINATIONS 2009/2010 ACADEMIC YEAR FOR THE CERTIFICATE OF BRIDGING MATHEMATICS 

## COURSE CODE: BMATH 001

COURSE TITLE: GEOMETRY AND VECTORS

STREAM:
DAY:
FRIDAY
TIME:
9.00-11.00 A.M.

DATE:
30/07/2010

## INSTRUCTIONS:

- Answer Question ONE and Any Other TWO Questions


## PLEASE TURN OVER

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## QUESTION 1(30 MARKS)

a) Define the term angle and state five types of angles
[3mks]
b) Find the size of an angle if it's five times its supplement
c) Find the value of $x, y, z$ in the figure below.

d) What do you call a regular polygon each of whose interior angle is $60^{\circ}$ and $90^{\circ}$ ? State the name of each.
e) Find the number of sides of a polygon each of whose exterior angle is $36^{\circ}$ and $60^{\circ}$. State the name of each.
f) Construct a regular pentagon of sides 4 cm .
g) Triangle RST is such that angle $\mathrm{RST}=53^{\circ}, \mathrm{ST}=10 \mathrm{~cm}, \mathrm{TR}=8 \mathrm{~cm}$. Construct the triangle and measure RS and angle TRS.
h) AB is the diameter of a circle such that the coordinate of $\mathrm{A}(1,1), \mathrm{B}(5,1)$ respectively. Find the centre and the radius of the circle hence state the equation of the circle.
i) The equation of a circle is $x-6 x+y+4 y=3$.Find the centre and radius. [3mks]
j) Find the area of a sector of a circle if $r=1.4 \mathrm{~cm}$ and angle is $30^{\circ}$

## OUESTION 2 (20 MARKS)

a) Two circles have radii 4 cm and 8 cm respectively. If they share a common chord of length 6 cm . Calculate the area of intersection of the two circles.
b) A minor sector of a circle of radius 28 cm includes an angle of $135^{\circ}$ at the centre .Find the area of the sector; the length of the minor arc, the sector is folded to form a right circular cone. Find the radius of the cone and height of the cone.
c) P and Q are the center of two circles with radii r 1 and r 2 . Construct the transverse common tangents to both sides.

## QUESTION 3 (20marks)

1) a) Consider the right pyramid below. Find the height of the pyramid, the slant height VM.If angle $0=90^{\circ} \mathrm{AO}$ is half the diagonal of the base rectangle ABCD and triangle VBC is an isosceles triangle.

b) Consider the regular tetrahedron of side 4 cm and midpoint M of RS :

i. Show that PM is $2 \sqrt{ } 3$ long and that triangle PMQ is isosceles
[3mks]
ii. Calculate the angle between planes PSR and QRS
iii. Calculate the angle between line PQ and plane QRS
c) Define the following:

| i. | Chord |
| ---: | :--- |
| ii. | Segment |
| iii. | Arc |

iv. Skew lines

## QUESTION 4 (20MARKS)

a) Find the values of $x$ and $y$ in the figure below:

b) Given that angle $\mathrm{CDX}=66^{\circ}$ and angle $\mathrm{ADT}=62^{\circ}$ and angle $\mathrm{BAC}=22^{\circ}$. Find angles ABD , ACD and angle BCD in the figure below
[5mks]

c) Construct a triangle PQR where $\mathrm{PQ}=8 \mathrm{~cm}$, angle $\mathrm{RPQ}=45^{\circ}$ and angle $\mathrm{PQR}=60^{\circ}$.Using a ruler and a pair of compasses only and inscribe a circle and measure its radius
d) OAB is a triangle in which $\mathrm{OA}=\mathrm{a} O B=\mathrm{b}$ and C divides B in the ratio 3:2 and divides OB in the ratio 1:2. OC meets AD at $S$.Given that $\mathrm{OS}=\mathrm{n} \mathrm{OC}$ and $\mathrm{AS}=\mathrm{m} A D$. Express OS in terms of $a$ and $b$ and hence find the values of $m, n, O S N$ and AS?

## QUESTION 5 (20 MARKS)

a) From a point P from the ground 15 M away from the foot of a building the angle of elevation of the top of the building is 20.Calculate the height of the building and the shortest distance of the top of the building from P .
[5mks]
b) Prove that $\mathrm{a} / \sin \mathrm{A}=\mathrm{b} / \sin \mathrm{B}=\mathrm{c} / \sin \mathrm{C}$ using sine rule
c) Solve for the lengths of the triangle .If $\mathrm{AC}=6 \mathrm{~cm}, \mathrm{BC}=14 \mathrm{~cm}$, if angle $\mathrm{A}=62^{\circ}$, angle $\mathrm{B}=58^{\circ}$, angle $\mathrm{C}=68^{\circ}$
[3mks]
d) Find the size of the smallest angle in the triangle below if $\mathrm{AC}=5 \mathrm{~cm}, \mathrm{AB}=6.5 \mathrm{~cm}, \mathrm{CB}=3.5 \mathrm{~cm}$
[3 mks]
e) A chord XY of length 12 cm is drawn in a circle centre O , radius 10 cm with midpoint M . Calculate the distance ON, area of triangle OXY, area of sector OXY, area of minor and major segment
[5mks]

