

**KABARAK**



**UNIVERSITY**

**UNIVERSITY EXAMINATIONS  
2010/2011 ACADEMIC YEAR  
FOR THE DEGREE OF BACHELOR OF EDUCATION  
SCIENCE**

**COURSE CODE: MATH 211**

**COURSE TITLE: LINEAR ALGEBRA I**

**STREAM:                   SESSION III & IV & V**

**DAY:                        TUESDAY**

**TIME:                     9.00 – 11.00 A.M.**

**DATE:                     12/04/2011**

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**INSTRUCTIONS:**

1. Answer question **ONE** and any other **TWO** questions
2. Begin each question on a separate page
3. Show your workings clearly

**PLEASE TURN OVER**

**QUESTION ONE (30 MARKS)**

- a) Find the determinant of  $A = \begin{pmatrix} 2 & -1 & 1 \\ -1 & 0 & 3 \\ 2 & 1 & -4 \end{pmatrix}$  (4 marks)
- b) Compute the inverse of the following matrices using row reduction method
- i)  $\begin{pmatrix} 3 & 1 \\ 5 & 2 \end{pmatrix}$  (3 marks)                      ii)  $\begin{pmatrix} 2 & -3 \\ 4 & 4 \end{pmatrix}$  (3 marks)
- c) Given  $v = (3, -1, -2)$  find the a unit vector that,
- i) Points in the same direction as  $v$  (3 marks)
- ii) Points in the opposite direction as  $v$  (2 marks)
- d) Find the angle between the vectors  $p = 2i + 3j + 4k$  and  $q = 4i - 3j + 2k$  (5 marks)
- e) Determine if the following sets of vectors will span  $R^3$
- i)  $v_1 = (2, 0, 1)$ ,  $v_2 = (-1, 3, 4)$  and  $v_3 = (1, 1, -2)$  (5 marks)
- ii)  $v_1 = (1, 2, -1)$ ,  $v_2 = (3, -1, 1)$  and  $v_3 = (-3, 8, -5)$  (5 marks)

**QUESTION TWO (20 MARKS)**

- a) Given  $u = (3, -1, 4)$  and  $v = (2, 0, 1)$  compute each of the following
- i)  $u \times v$  and  $v \times u$  (6 marks)
- ii)  $u \times u$  (2 marks)
- iii)  $u \cdot (u \times v)$  and  $v \cdot (u \times v)$  (4 marks)
- iv) Angle between  $u$  and  $v$  (4 marks)
- b) Find the rank of the following matrix
- $\begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 2 & 1 & 0 \end{pmatrix}$  (4 marks)

QUESTION THREE (20 MARKS)

- a) Given  $u = (-2, 3, 1, -1)$  and  $v = (7, 1, -4, -2)$  verify the cauchy-schwarz inequality and the triangular inequality (6 marks)
- b) Determine if the following sets of vectors are linearly independent or linearly dependent
- i)  $v_1 = (1, 1, -1, 2)$ ,  $v_2 = (2, -2, 0, 2)$  and  $v_3 = (2, -8, 3, -1)$  (5 marks)
- ii)  $v_1 = (1, -2, 3, -4)$ ,  $v_2 = (-1, 3, 4, 2)$  and  $v_3 = (1, 1, -2, -2)$  (5 marks)
- c) Show that  $(A^n)(A^{-1}) = I$  (4 marks)

QUESTION FOUR (20 MARKS)

- a) Suppose that  $u = (u_1, u_2, u_3)$  and  $v = (v_1, v_2, v_3)$  are two vectors in 3- space then, Show that  $u \cdot v = u_1v_1 + u_2v_2 + u_3v_3$  (7 marks)
- b) Solve the following systems of equations using crammers rule
- $4x + 2y + 4z = 16$
- $2x - 6y + 6z = -8$  (7 marks)
- $8x + 4y - 2z = 2$
- c) Evaluate each of the following if  $A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$
- i)  $A^2$  (3 marks)
- ii)  $A^3$  (3 marks)

QUESTION FIVE (20 MARKS)

a) For the following matrices compute

$$A = \begin{bmatrix} 1 & -2 & 3 \\ 2 & 7 & 4 \\ 3 & 1 & 4 \end{bmatrix}$$

$$B = \begin{bmatrix} 1 & 0 & 5 \\ 7 & -3 & 4 \\ 2 & -1 & -4 \end{bmatrix}$$

- i) Det(A) (3 marks)
  - ii) Det(B) (3 marks)
  - iii) Det(AB) (3 marks)
  - iv) Det  $A^{-1}$  (2 marks)
- b) Show that  $u = (3, 0, 1, 0, 4, -1)$  and  $v = (-2, 5, 0, 2, -3, -18)$  are orthogonal and verify that the pythagorean Theorem holds (8 marks)