## KENYA METHODIST UNIVERSITY <br> END OF SECOND TRIMESTER 2006/2007 EXAMINATIONS

FACULTY : SCIENCES
DEPARTMENT : MATHEMATICS AND COMPUTER SCIENCE
COURSE CODE : MATH 134
COURSE TITLE : INFERENTIAL STATISTICS
TIME : 3 HRS

## Instructions:

- Answer question 1 (compulsory) and any other 2 questions.


## Question 1

a) Briefly explain the steps used in testing of hypothesis.
b) For the purpose of calculating the dosage for a certain disease, a doctor uses the normal distribution for adult patients with mean 150 and standard deviation 20 pounds. To check this claim, 49 patients were randomly selected and weighed; calculate probability of patients in that sample that:
i) Weigh less than 148 pounds
ii) Between 145 and 176 pounds.
c) An assembly operation in a manufacturing plant requires approximately a 1 month training period for a new employee to reach maximum efficiency. A new method of training was suggested and a test was conducted to compare the new and standard methods. Two groups fo nine new employees were trained for a period of 3 weeks, one group using the new method and the other using the standard method. The length of time (in minutes) required for each employee to assemble the devices was recorded at the end of 3 weeks period.

| Standard method | 32 | 27 | 35 | 28 | 41 | 44 | 35 | 31 | 34 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| New method | 35 | 31 | 29 | 25 | 34 | 40 | 27 | 32 | 31 |

At 5\% level of significance, is there sufficient evidence to indicate a difference in true mean times for the two methods?
( 7 mks )
d) The data below gives the values for 12 births of the birth weight ( x ) and the increase in weight between 70 and 100 of life, expressed as a percentage of the birth weight (y).

| $\mathrm{x}(\mathrm{oz})$ | 112 | 111 | 107 | 119 | 92 | 80 | 81 | 84 | 118 | 106 | 103 | 94 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{y}(\%)$ | 63 | 66 | 72 | 52 | 75 | 118 | 120 | 114 | 42 | 72 | 90 | 91 | You may use the following totals:

$$
\sum x=1207 \quad \sum y=975 \quad \sum x y=94322 \quad \sum x^{2}=123561 \quad \sum y^{2}=86487
$$

i) Calculate the sample correlation coefficient between x and y .
ii) Test whether there is a linear correlation between x and y at $10 \%$ level of significance.
e) Differentiate between the terms:
i) Parameter and statistics.
ii) Non parametric and parametric tests.

## Question 2

a) The following sample of 26 measurements was selected from a population that is normally distributed

| 91 | 80 | 99 | 110 | 95 | 106 | 78 | 121 | 106 | 100 | 97 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 82 | 100 | 83 | 115 | 104 | 114 | 118 | 96 | 101 | 79 | 101 |
| 79 | 130 | 94 | 101 |  |  |  |  |  |  |  |

## Calculate:

i) Standard error
ii) $98 \%$ confidence interval for the true mean.
b) Jane believes that there is no difference in proportions of degrees for both male and female graduates. A random sample of 200 university degrees earned in 2006 gave the following breakdown.

|  | Degree Earned <br> Gender |  | Bachelor |
| :--- | :--- | :--- | :--- | Masters $\quad$ Doctorate

Test whether there is a relationship between degree earned and gender at 5\% level of significance.

## Question 3

Six samples of each of the four types of cereal grains grown in a certain region were analyzed to determine the thiamine content resulting in the following

| Wheat | 5.2 | 4.5 | 6.0 | 6.1 | 6.7 | 5.8 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Barley | 6.5 | 8.0 | 6.1 | 7.5 | 5.9 | 5.6 |
| Maize | 5.8 | 4.7 | 6.4 | 4.9 | 6.0 | 5.2 |
| Oats | 8.3 | 6.1 | 7.8 | 7.0 | 5.5 | 7.2 |

Carry out analysis of variance and test whether the mean thiamine content for the cereals is the same at $10 \%$ of significance.
(20 mks)

## Question 4

a) The percentage of ideal body weight was determined for randomly selected insulin-dependent diabetics. The outcomes are as follows:

| 107 | 119 | 99 | 114 | 120 | 104 | 124 | 88 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 114 | 116 | 101 | 121 | 152 | 125 | 100 | 95 |
| 117 |  |  |  |  |  |  |  |

Construct a $98 \%$ confidence interval for variance in the percentage of ideal body weight. ( 10 mks )
b) Independent random samples of three different brands of magnetron tubes were subjected to stress testing the number of hours each operated without repair was recorded. Experience has shown that the distributions of life length for manufactured products are often non-normal and thus proper use of an ANOVA f-test.

| Brand A | Brand $B$ | Brand $C$ |
| :--- | :--- | :--- |
| 36 | 49 | 7 |
| 48 | 33 | 31 |
| 5 | 60 | 140 |
| 67 | 2 | 59 |
| 53 | 55 | 42 |

Use the Kruskal-Wallis H - test to determine whether evidence exists to conclude that the brands of magnetron tubes tend to differ in length of life under stress at $5 \%$ level of significance. (10 mks)

