## KENYA METHODIST UNIVERSITY <br> END OF SECOND TRIMESTER 2006/2007 EXAMINATIONS

FACULTY : SCIENCES
DEPARTMENT : MATHEMATICS AND COMPUTER SCIENCE
COURSE CODE : MATH 430
COURSE TITLE : OPERATIONS RESEARCH II
TIME : 3 HRS
Instructions: Attempt Question 1 (compulsory) and any other three questions.
Question 1 (25 marks)
a) Define a cut.
(2 mks)
b) Determine two cuts and their capacities in the network below.

c) Determine the maximum flow and the optimal flow for the above network.

## Question 2 ( 15 marks)

The Telkom cable company is in the process of providing cable services to five new housing projects. The figure below depicts the potential cable linkages to the 5 projects. The cable distances (in Km) are shown on each branch. Determine the most economical cable network using the minimal spanning tree Algorithm.


## Question 3 (15 marks)

Three steel works I, II and III produce 50, 50 and 100 tonnes of steel per week. The steel has to be transported to consumers A, B, C and D whose demands are 30, 40, 60 and 70 tonnes respectively. The cost of transportation is thousands of Kenya shillings from the producers to the consumers are listed below:

|  | $\boldsymbol{A}$ | $\boldsymbol{B}$ | $\boldsymbol{C}$ | $\boldsymbol{D}$ |
| :--- | :--- | :--- | :--- | :--- |
| I | 15 | 7 | 20 | 10 |
| II | 12 | 8 | 11 | 20 |
| III | 9 | 16 | 12 | 15 |

Starting with the basic solution obtained by the North West corner method, determine the optimal solution.

## Question 4 (15 marks)

There are five pumps available for developing wells. The efficiency of each pump in producing maximum yield at each well is given in the table below:

|  | 1 | 2 | 3 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 45 | 40 | 65 | 30 | 55 |
| 2 | 50 | 30 | 25 | 60 | 30 |
| 3 | 25 | 20 | 15 | 20 | 40 |
| 4 | 35 | 25 | 30 | 25 | 20 |
| 5 | 80 | 60 | 60 | 70 | 50 |

Determine in what way should the pumps be assigned to maximize the overall efficiency using the Hungarian method.

Question 5 ( 15 marks)
a) What is the major difference between CPM and PERT.
b) Distinguish between a critical and a non-critical activity.
c) Consider the project network below:

i) Determine the critical path and the associated critical path and the associated critical activities of this project.
ii) How long will it take to complete the project?
iii) Construct a time schedule for the project.

