



CHEPKOILEL UNIVERSITY COLLEGE

(A CONSTITUENT COLLEGE OF MOI UNIVERSITY)

UNIVERSITY EXAMINATIONS 2011/2012 ACADEMIC YEAR FIRST SEMESTER REGULAR EXAMINATIONS

FOR THE DEGREE OF BACHELOR OF SCIENCE IN ACTUARIAL SCIENCE

COURSE CODE: ACS 101

**COURSE TITLE: INTRODUCTION TO
ACTUARIAL SCIENCE**

DATE: 30TH NOVEMBER, 2011 TIME: 2.00 P.M – 5.00 P.M

INSTRUCTIONS TO CANDIDATES

- SEE INSIDE

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CHEPKOILEL UNIVERSITY COLLEGE

ACS 101 : INTRODUCTION TO ACTUARIAL SCIENCE-2011/2012

SECTION A (Attempt all Questions)

Question 1

a) Suppose you have borrowed a five year loan of Ksh 100,000 at 10 per cent from your employer to buy a motor cycle. If your employer requires a five equal end of year repayments, then what will be?

- (i) Annual installment.
- (ii) Annual interest.
- (iii) Principal repayment.
- (iv) Outstanding balance.

(7 marks)

b) With the help of examples differentiate between pure and speculative risks.

(5 marks)

- c) (i) Given $i = 0.1$ calculate the value of d and v .
- ii) Given $d = 0.05$ calculate the value of i and v
- iii) Given $v = 0.08$ calculate the value of i and d .

(4 marks)

Question 2

a) The distribution of fire damage to the ware house belonging to Z Company is shown below.

Amount in ksh	Probability
0	0.6
20,000	0.2
80,000	0.1

85,000	0.08
100,000	0.01
160,000	0.01

It is the policy of the company to insure fire risks if premiums charged do not exceed 20% of the expected loss, otherwise the risks are retained.

- i) As a risk manager, advise the company on the course of action with regard to the fire risk if cost for fire insurances is Ksh. 4,000.
- ii) What is the probability of losses exceeding Ksh. 90,000?

(7 marks)

b) What do you understand by the term enterprise risks?

(8 marks)

Section B. (Attempt any 3 questions)

✓ **Question 3**

(a) The following is an extract from ELT table

Age x	l_x	d_x	$P_x [T] = x$
30	10,000	34.78	-
31	9965.22	38.1	-
32	9927.12	41.76	-
33	9885.35	45.80	-
34	9839.55	50.26	-
35	9789.29	55.17	-
36	9734.12	60.56	-

37	9673.56	66.49	-
38	9607.07	72.99	-
39	9534.08	80.11	-

Complete the Table by calculating for $P_x [T] = x$ for $x = 30, 31, 32, 33, 34, 35, 36, 37, 38, 39$ and 40 for a randomly selected individual from the age 30.

(5 marks)

(b) Using the table in part (a) calculate the following

Probabilities

- (i) Prob [35 dies after 3 years]
- (ii) Prob [30 survived for 3 years]
- (iii) Prob [36 survived 2 years then dies the following year]

(5 marks)

c) Define the symbols l_x , d_x and P_x

(3 marks)

✕ Question 4

- a) Describe the cash flow model for each of the following cases.
 - i) Pensions.
 - ii) Endowment assurance.
 - iii) Deductibles.
 - iv) Principle of indemnity.

(8 marks)

b) If 110,000 items shipped by the firm only 110 were damaged in transit. What is the probability of having 0, 1, 2, and 4 damaged items in a sample of 900, items.

(5 marks)

✓ Question 5 Investment in project A and B.

Economic Conditions	probability	returns %	
		A	B
Good	0.5	40	0
Bad	0.5	0	40

- Calculate the expected rate of return, variance and standards deviation of A.
- Calculate the expected rate of return, variance and standard deviation of B.
- Calculate expected portfolio return of A and B.

(6 marks)

- Differentiate between systematic and unsystematic risks.

(2 marks)

(ii) Suppose Ksh. 10,000 is placed in the saving account of a bank at 10% percent interest rate. Calculate A_c and A_s at the end of five years and comment on the differences.

(5 marks)

Question 6

- (a) The risk free rate of interest is 9%. The market portfolio is expected to yield a return of 20% with standard deviation of 6%. Calculate the expected portfolio rate of return if the standard deviation of portfolio is 5%.

(4 marks)

- (b) Let $A_c(i,n)$ and $PV(i,n)$ denote the function for accumulation of amount 1 for n years at the rate of interest i per annum, under compound interest and present value investment model respectively. Determine, in terms of i and n the expression for $A_c(i,n)$ and $PV(i,n)$.

(4 marks)

- (c) The following is an extract of ELT table

Ages x	l_x	dx
0	1000	200
1	800	150
2	650	100
3	550	150
4	400	100

Find

$$l_2$$

$${}_2P_2$$

$$q_3$$

(5marks)

7. (a) In tossing a coin 1000 times. Find the probability of obtaining less than 470 heads.

(6 marks)

b) How many years does it take for money to triple in value at interest rates i ?

Given t [$i=0.05$, $i=0.07$, $i=0.1$]

(4 marks)

c) Define the following symbols d and v .

(3 marks).