# JARAMOGI OGINGA ODINGA UNIVERSITY OF SCIENCE AND TECHNOLOGY 

## DIPLOMA IN LOGISTICS

MAY-AUGUST 2014 SEMESTER
MAIN EXAMINATION

## FUNDAMENTALS OF OPERATIONS RESEARCH

## DURATION; 2 HOURS

## INTRUCTIONS; ANSWER QUESTION ONE AND ANY OTHER TWO

## SECTION A

1. a) What is meant by operations research? ( 2 marks)
b) What are the essential features of linear programming problems? ( 6 marks)
c) Explain the meaning of the terms:
i) Objective function ( 2 marks)
ii) Constraints ( 2 marks)
d) Solve the following quadratic equations.
i) $\quad 6 x^{2}+8 x+2=0$ (3 marks)
ii) $\quad 6 x^{2}-x-2=0 \quad$ (3 marks)
e) Differentiate between a finite and an infinite set (4 marks)
f) If $U=(1,2,3,4,5,6,7), A=(1,4,6,7)$, find $A$ (2 marks)
g) Differentiate the following functions.
i) $y=x^{3}$
ii) $y=x^{5 / 3}$
(2 marks)
iii) $y=\sqrt{ } x$
(2 marks)
SECTION B $\}$
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2. A research was conducted on Gretsa University students to test their interest in three subjects; Mathematics; Business statistics; and Communication skills. It was noticed that 35 students are interested in Mathematics, 20 are interested in Business statistics and 20 are interested in Communication skills. Out of them, 7 are interested in both mathematics and Business statistics, 4 are interested in both business statistics and communication skills, 6 are interested in both mathematics and communication skills and 2 are interested in all the three subjects. Find out the total number of students. (20 marks).
3. A firm produces two products X and Y with a contribution of Kes 8 and Kes 10 per unit respectively. Product data is as follows ( per unit);

|  | Labour hours | Material A | Material B |  |
| :--- | :---: | :--- | :--- | :--- |
| X | 3 | 4 | 6 |  |
| Y | 5 | 2 | 8 |  |
|  |  |  |  |  |
| Total available |  | 500 |  | 350 |
|  |  |  | 800 |  |

a) Formulate the LP model
b) Solve the problem graphically
c) Calculate the shadow prices of the binding constraints and interpret. ( 20 marks)
4. The cost of producing $x$ units in a firm is given as; total cost $(T C)=$ $x^{2}+6 x+18$. The price per unit is Kes 20.
i) Find the profit function
ii) How much profit will the firm make if it produces 50 units? (5marks)
5. A factory produces four products $\mathrm{A}, \mathrm{B}, \mathrm{C}$ and D which earn contributions of Kes 20 , Kes 25 , Kes 12 and Kes 30 per unit respectively. The factory employs 500 workers who work a 40 hour week. The times required for each product and the material requirements are set out below.

Products

$$
\begin{array}{llll}
\mathrm{A} & \mathrm{~B} & \mathrm{C} & \mathrm{D}
\end{array}
$$

$\begin{array}{lllll}\text { Hours per unit } & 6 & 4 & 2 & 5\end{array}$
Kg material X/unit
$\begin{array}{llll}2 & 8.3 & 5 & 9\end{array}$
$\begin{array}{lllll}\text { Kg material y/unit } & 10 & 4 & 8 & 2\end{array}$
$\begin{array}{lllll}\text { Kg material z/unit } & 1.5 & 0 & 2 & 8\end{array}$

Total available materials per week is $\mathrm{X}=100,000 \mathrm{kgs}, \mathrm{Y}=65,000 \mathrm{kgs}, \mathrm{Z}=$ $220,000 \mathrm{kgs}$

The company wishes to maximize contribution.
a) Formulate the PL problem in the standard manner. ( 8 marks)
b) State the two advantages and two disadvantages of simulation. (4 marks)
c) Explain four features of a good model in operations research ( 8 marks)

