



**JARAMOGI OGINGA ODINGA UNIVERSITY OF SCIENCE  
AND TECHNOLOGY  
UNIVERSITY EXAMINATION 2013  
1ST YEAR 2ND SEMESTER EXAMINATION FOR THE  
DEGREE OF BACHELOR OF EDUCATION ARTS WITH IT  
(S BASED KOSELE)**

**COURSE CODE: SMA 208**

**TITLE: ANALYSIS**

**DATE: 4/5/2013**

**TIME: 15.00-17.00PM**

**DURATION: 2 HOURS**

**INSTRUCTIONS**

- 1. This paper contains FIVE (5) questions**
- 2. Answer question 1 (Compulsory) and ANY other 2 Questions**
- 3. Write all answers in the booklet provided**

### QUESTION 1

- (a) Differentiate between infinite and a finite set. **(2mks)**
- (b) Define a null set. **(1mk)**
- (c) If  $A=(3,4)$   $B= (2,4,6,8)$ . Find  $A \cup B$ . **(2mks)**
- (d) (i) Define the term neighbourhoods of a set. **(2mks)**  
(ii) If  $M$  and  $N$  are neighbourhood of a point  $X$ , then show that  $M \cap N$  is also a neighbourhood of  $X$ . **(6mks)**
- (e) Prove that the greatest member of a set, if it exists, is the supremum (l.u.b) of the set. **(5mks)**
- (f) Let  $A$ ,  $B$  and  $S$  be sets of real numbers. Show that
- (i)  $\underline{S} \subseteq \bar{S}$  **(4 marks)**
- (ii)  $\underline{A \cap B} = \bar{A} \cap \bar{B}$  **(4 marks)**
- (iii)  $\bar{S}$  is always closed **(4 Marks)**

### QUESTION 2

- (a) Define
- (i) Interior point of a set  $S$ . **(1mk)**
- (ii) Interior of a set  $S$ . **(1mk)**
- (iii) Open sets. **(2mks)**
- (b) Show that every open set  $S$  is a union of open intervals. **(5mks)**
- (c) Prove that interior of a set  $S$  is an open set. **(10mks)**
- (d) Define a closed set  $S$ . **(3mks)**

### QUESTION 3

- (a) Show that for every three non-empty sets  $R$ ,  $S$ ,  $T$  we have  
 $R \cap (S \cup T) = (R \cap S) \cup (R \cap T)$  **(10mks)**
- (b) State and prove the De Morgans Law. **(10mks)**

#### QUESTION 4

- (a) Give the definition of limit of a function and prove that this limit is unique. **(5mks)**
- (b) Define the concept of uniform continuity. Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be defined by  $f(x) = x$  for all  $x$  in  $\mathbb{R}$ . Show that  $f$  is uniformly continuous on  $\mathbb{R}$ . **(5mks)**
- (c) (i) Given  $f(x) = x^2 - 5x$ , show that  $\lim_{x \rightarrow -6} f(x) = -6$ . **(2mks)**
- (ii) Determine a value for  $\delta > 0$  associated with  $\epsilon > 0$  in accordance with the definition of limit of a function. **(8mks)**

#### QUESTION 5

- (a) Define a field on a set  $S$ . **(5mks)**
- (b) Let  $x$  and  $y$  be positive real numbers. Show that:
- (i)  $x+y$  is also positive
  - (ii)  $x < y$  iff  $x^2 < y^2$
  - (iii)  $x < y^{1/y} < 1/x$  **(15mks)**