COLLEGE

## UNIVERSITY EXAMINATIONS

THIRD YEAR EXAMINATION FOR THE AWARD OF DEGREE OF BACHELOR OF SCIENCE (ECONOMICS \& STATISTICS)

## MATH 346: APPLIED STATISTICS

STREAM: ECON \& STAT Y3S
DAY/DATE: TUESDAY 18/12/2012
TIME: 2 HOURS
8.30 A.M. - 10.30 A.M

## INSTRUCTIONS:

## Answer question one and any other two

Question 1 (30 Marks)
(a) Differentiate between the following terms;
(i) Sampling distribution and probability distribution of a variable.
(ii) Type 1 and type 11 error
(iii) One tailed test and two tailed test.
[6 Marks]
(b) State and explain the basic principles of experimental designs.
(c) Differentiate between simple random sampling and convenient sampling.
(d) State the major steps in testing a hypothesis.
(e) State and explain the major differences between:
(i) Kruskal Wallis H. test and sign test.
(ii) Mann Whitney test and chin square test.
(f) Explain the meaning of mean square error and standard error as used in multiple regression model.

## Question Two (20 Marks)

Breast cancer is emerging to be a major threat to the population in Kenya. It is also emerging that the disease affects both male and female. A chukka nursing student has interviewed a number of residents of Nithi village about their cancer status and present $s$ the following data.

| Breast cancer status | Gender |  |
| :--- | :--- | :--- |
|  | Male | Female |
| Positive | 40 | 70 |
| Negative | 60 | 50 |
| Unknown | 120 | 40 |
|  |  |  |

You are required to:
(a) At the 5\% level of significance, determine if cancer status is independent of gender.
(b) Four treatments were compared using a completely randomized design. The data is as shown in the table below.

| Treatments |  |  |  |
| :---: | :---: | :---: | :---: |
| 1 | 2 | 3 | 4 |
| 124 | 147 | 141 | 117 |
| 167 | 121 | 144 | 128 |
| 135 | 136 | 139 | 102 |
| 160 | 114 | 162 | 119 |
| 159 | 129 | 155 | 128 |
| 144 | 117 | 150 | 123 |
| 133 | 109 |  |  |

Does the data provide sufficient evidence to indicate a difference in location from at least two of the population? Test using the Kruskal - Wallis H statistic, with $\alpha=0.05$.
[10 Marks]

## Question Three (20 Marks)

The issue of income distribution in Kenya is being debated in the wake of the proposed devolved system of governance. Momanyi has obtained income data for 9 residents in each of the 4 counties of interest to him. The data is presented in the table below. Perform an ANOVA test at $5 \%$ significance to determine if the mean income in the 4 counties is equal.
[20 Marks]

| Nyeri | Kakamega | Kisumu | Garissa |
| :--- | :--- | :--- | :--- |
| 34 | 45 | 20 | 12 |
| 45 | 34 | 25 | 109 |
| 67 | 42 | 34 | 39 |
| 56 | 24 | 57 | 49 |
| 89 | 45 | 88 | 38 |
| 32 | 90 | 47 | 26 |
| 12 | 23 | 34 | 22 |
| 23 | 78 | 32 | 45 |
| 65 | 18 | 20 | 20 |

## Question Four (20 Marks)

(a) From the set of data given below

| $\mathrm{X}_{\mathrm{i}}$ | 28.0 | 28.0 | 32.5 | 39.0 | 45.9 | 57.8 | 58.1 | 62.5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{Y}_{\mathrm{i}}$ | 12.4 | 11.7 | 12.4 | 10.8 | 9.4 | 9.5 | 8.0 | 7.5 |

(i) Compute the least square estimates of the regression parameters $\beta_{0}$ and $\beta_{0}$.
(ii) Test the hypothesis $H_{0}: \beta_{1}=0$ vs $H_{1}: \beta_{1} \neq 0$ at $5 \%$ level of significance.
(b) The average time before the gear train of a certain make of automobile needs a major overhaul is 56 months, with a standard deviation of 16 months. The manufacturer wishes to warranty these gear trains, offering to make any necessary overhaul free of charge if the buyer of a new automobile has a gear-train breakdown before a certain number of months of ownership have elapsed. Assume that the number of months before an overhaul is required is normally distributed. For how many months should the manufacturer warrant the gear trains to limit the number of warranty overhaul, to no more than $2.28 \%$ of the automobiles sold?
[6 Marks]

