MERU UNIVERSITY OF SCIENCE AND TECHNOLOGY
P.O. Box 972-60200 - Meru-Kenya.

Tel: 020-2069349, 061-2309217. 064-30320 Cell phone: +254 712524293, +254 789151411
Fax: 064-30321
Website: www.must.ac.ke Email: info@mucst.ac.ke

## University Examinations 2013/2014

SECOND YEAR, SECOND SEMESTER EXAMINATION FOR THE DEGREE OF BACHELOR OF COMMERCE

HBC 2210/2122: OPERATIONS RESEARCH I
DATE: DECEMBER 2013
TIME: 2HOURS
INSTRUCTIONS: Answer question one and any other two questions

## QUESTION ONE - (30 MARKS)

a) Write a brief history of operation research.
b) Find the dual linear program of

$$
\begin{aligned}
\text { minimize } & z=20 x_{1}+30 x_{2} \\
\text { Subject to: } & 2 x_{1}+x_{2} \leq 80 \\
& x_{1}+2 x_{2} \leq 60 \\
& x_{1} \geq 10, x_{2} \geq 15
\end{aligned}
$$

c) Solve the following linear programming problem using simplex method
maximize $z=60 x_{1}+40 x_{2}$
Subject to: $7 x_{1}+8 x_{2} \leq 1600$

$$
8 x_{1}+12 x_{2} \leq 1600
$$

$$
15 x_{1}+16 x_{2} \leq 1600
$$

$$
\begin{equation*}
x_{1}, x_{2} \geq 0 \tag{10Marks}
\end{equation*}
$$

d) Find the initial basic feasible solution to the following transportation problem using least cost entry method.
(9 Marks)

| Source | Destination |  |  | Available |
| :--- | :--- | :--- | :--- | :--- |
|  | 1 | 2 | 3 |  |
|  | 50 | 30 | 190 | 10 |
|  | 80 | 45 | 150 | 30 |
|  | 220 | 180 | 50 | 40 |
| Requirement | 40 | 20 | 20 |  |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |

e) At a certain refinery, the refining process requires the production of at least two gallons of petrol for each gallon of crude oil. To meet the anticipated increased fuel demands, at least 3 million gallons of crude oil a day needs to be produced. The demand for petrol on the other hand, is not more than 6.4 million gallons a day. If petrol is selling at $\$ 1.90$ per gallon and crude oil sells for $\$ 1.50$ per gallon. Formulate the underlying linear programming problem that seeks to find how much of each should be produced in order to maximize revenue.

## QUESTION TWO - (20 MARKS)

A company wants to supply materials from three plants to three new projects. Project I requires 50 truck loads, project II requires 40 truck loads and project III requires 60 truck loads. Supply capacities for the plants $\mathrm{P}_{1}, \mathrm{P}_{2}$ and $\mathrm{P}_{3}$ are 30,55 and 45 truck loads.

The table of transportation costs and initial BFs using Vogels' approximation method is given in the table below

| From |  | To |  |  |  |
| :--- | ---: | ---: | ---: | ---: | :---: |
|  |  | I | II | III |  |
|  | $\mathrm{P}_{1}$ | 7 | 10 | 12 |  |
|  | $\mathrm{P}_{2}$ | 8 | 12 | 7 |  |
|  | $\mathrm{P}_{3}$ | 4 | 9 | 10 |  |
|  | $\mathrm{P}_{4}$ | 0 | 0 | 0 |  |

Find the optimal solution.

## QUESTION THREE (20 MARKS)

a) A company is faced with the problem of assigning 4 jobs to 5 persons. The expected profit in rupees for each person on each job are as follows

| Persons | Job |  |  |  |
| :---: | :--- | :--- | :--- | :--- |
|  | $\mathbf{J}_{1}$ | $\mathbf{J}_{2}$ | $\mathbf{J}_{3}$ | $\mathbf{J}_{4}$ |
| I | 86 | 78 | 62 | 81 |
| II | 55 | 79 | 65 | 60 |
| III | 72 | 65 | 63 | 80 |
| IV | 86 | 70 | 65 | 71 |
| V | 72 | 70 | 71 | 60 |

Find the assignment of persons to jobs that will result in a maximum profit.
(10 Marks)
b) Goods have to be transported from source $S_{1}, S_{2}$ and $S_{3}$ to destinations $D_{1}, D_{2}$ and $D_{3}$. The transportation cost per unit, capacitances of the sources and requirements of the destinations are given in the following table.

|  | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ | Capacity |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{S}_{1}$ | 8 | 5 | 6 | 120 |
| $\mathrm{~S}_{2}$ | 15 | 10 | 12 | 80 |
| $\mathrm{~S}_{3}$ | 3 | 9 | 10 | 80 |
|  | 150 | 80 | 50 |  |

Obtain the initial basic feasible solution using North - West Corner Rule.

## QUESTION FOUR (20 MARKS)

a) Arrivals at a service counter are considered Poisson with an average time of 10 minutes between arrivals. The length of service is assumed to be distributed exponentially with a mean of 3 minutes.
i. Calculate the utilization of the counter.
ii. What is the average time spends in the system.
b) A fast food canteen serves food to university students over lunch hour. On busy days, the canteen receives students at a rate of 140 per hour. Each students order takes 25 seconds to put together and to have it served. Assuming that students arrivals are Poisson distributed with exponential service rate in a single counter $(m|m| 1 \mid)$. Determine
i. Proportion of time that the counter is busy.
ii. Average number of students in the system.
iii. Average number of students in the queue.
iv. Average time spent in the system.

## QUESTION FIVE (20 MARKS)

a) Explain the following terms as used in network analysis
i. Loops and dangling.
ii. Critical path
iii. Optimistic time
iv. Pessimistic time
b) A project has been broken down into 10 activities with the following predecessors and duration.

| Activity | Predecessor | Duration (weeks) |
| :--- | :--- | :--- |
| A | - | 5 |
| B | - | 7 |
| C | A,B | 8 |
| D | - | 10 |
| E | C | 10 |
| F | B | 5 |
| G | C,F,H | 8 |
| H | D | 12 |
| I | D | 7 |
| J | I | 9 |

Draw the network diagram and identify the critical path.

