COLLEGE

## UNIVERSITY EXAMINATIONS

## SECOND YEAR EXAMINATION FOR THE AWARD OF DEGREE OF BACHELOR OF SCIENCE IN AGRIBUSINESS MANAGEMENT

## ECON 232: MATHEMATICS FOR ECONOMISTS

STREAM: B.SC(AGBM) Y2S1
DAY/DATE: TUESDAY 27/7/2010

## INSTRUCTIONS

Answer question One and any other two questions. Do not write on the question paper.

1. (a) Compute the following:
(i) $\quad \log _{5}\left(\sqrt{5^{10}}\right)\left(5^{-2}\right)$
(ii) $\quad\left(\frac{x^{-1 / 3}}{x^{-2 / 3}}\right)$
(iii) $(a+b)^{7}$
[3 marks]
(b) (i) What is an economic model?
[1 mark]
(ii) Consider the following national income model for an economy with no external trade.
$\mathrm{Y}=\mathrm{C}+\mathrm{I}+\mathrm{G}$
Where:
$\mathrm{C}=120+0.8 \mathrm{Y}$
$\mathrm{G}=40$

Find (a) Equilibrium income
[2 marks]
(b) Equilibrium consumption
[2 marks]
(iii) Find the equilibrium price and quantity for the following market model.

$$
\begin{aligned}
& \mathrm{Q}_{\mathrm{d}}=\frac{16}{P} \\
& \mathrm{Q}_{\mathrm{S}}=2 \mathrm{P}^{2}
\end{aligned}
$$

(c) The average total costs of a firm is given by:

$$
\mathrm{ATC}=\alpha_{1} \mathrm{Q}^{2}-\alpha_{2} \mathrm{Q}+\beta_{1}+\frac{\beta}{Q}
$$

Determine
(i) The total cost function for the firm.
[2 marks]
(ii) The fixed cost function for the firm.
(iii) The average variable and the average fixed functions for the firm.
[2 marks]
(iv) Sketch the graph of the average fixed cost function. [1 mark]
(d) You are provided with the following TR and TC functions.

$$
\begin{aligned}
& \mathrm{TR}=\mathrm{AQ}-\mathrm{bQ}^{2} \\
& \mathrm{TC}=\mathrm{F}+\mathrm{dQ}
\end{aligned}
$$

(i) Determine the profit function.
(ii) If $\mathrm{a}=9, \mathrm{~b}=2, \mathrm{~d}=2$ and $\mathrm{F}=3$, Find the level of Q for which profits are zero.
(e) Find $\frac{d y}{d x}$ for the function $y=(4 x)^{3}$
Q. 2 (a) Consider the production function:

$$
\mathrm{Q}=\mathrm{AL}^{\alpha} \quad 0<\alpha 1^{;} \mathrm{A}>0
$$

(i) Find the MPL
(ii) Express MPL in terms of $\alpha, \mathrm{L}$ and Q .
(iii) Determine the slope of MPL.
(iv) What is the sign of the slope of MPL?
[2 marks]
(v) Determine whether MPL increases, diminishes or remains constant as $L$ increases.
(b) Consider the following function:

$$
h(x)=\frac{1}{3} x^{3}+x^{2}-35 x+10
$$

Determine the critical values and find out whether these critical values are maxima or minima. Determine the extreme values of the function.
[10 marks]
Q. 3 (a) Consider the following utility function:

$$
U=25 x^{2 / 5} y^{3 / 5}
$$

(i)
(a) Find the MUx and MUy
[6 marks]
(b) From your results, find the MRCS between the two goods. [3 marks]
(ii) (a) By setting $\mathrm{U}=100$, derive the corresponding indifference curve.
[2 marks]
(b) Find the MRCS for $x=2$.
[2 marks]
(c) Does the indifference curve obey the Law of diminishing MRCS?
[1 mark]
(b) Find the MPC and MPS for the following function:

$$
\begin{equation*}
S=-150+0.25 Y \tag{3marks}
\end{equation*}
$$

(c) You are given the following information regarding demand and supply functions:

Demand function

$$
4 P+2 Q-40=0
$$

Supply function

$$
\mathrm{P}=2 \mathrm{Q}^{2}+4 \mathrm{Q}+2
$$

Determine:
(i) The marginal revenue function.
(ii) The marginal revenue at $\mathrm{Q}=10$
[1 mark]
4. (a) The commodity and money markets for an economy are defined by the following equations:

Commodity market

$$
\begin{aligned}
& \mathrm{Y}=\mathrm{C}+\mathrm{I} \\
& \mathrm{C}=200+\frac{2}{5} \mathrm{Y} \\
& \mathrm{I}=1900-12 \mathrm{r} \\
& \text { Money market } \\
& \mathrm{M}_{\mathrm{DT}}=\frac{1}{2} \mathrm{Y} \\
& \mathrm{M}_{\mathrm{DS}}=100-10 \mathrm{r} \\
& \mathrm{M}_{\mathrm{S}}=1500
\end{aligned}
$$

(i) Derive the IS and LM function for the economy. [2 marks]
(ii) What is the equilibrium income and rate of interest for the economy?
(b) Write short notes on the following:
(i) Local maxima and minima.
(ii) Global maxima and minima.
(iii) End point extrema.
[3 marks]
(c) Determine the derivatives of:
(i) $y=3 x^{2}\left(4 x^{3}+x^{2}\right)$
[2 marks]
(ii) $y=2 x^{3 / 4}-3 x^{2 / 3}+16$
[2 marks]
(iii) $\frac{x^{1 / 3}}{2+x^{5}}$
[2 marks]

