## University Examinations 2012/2013

FIRST YEAR, FIRST SEMESTER EXAMINATION FOR MASTER OF SCIENCE IN ENTREPRENUERSHIP

HR 3107: STATISTICS
DATE: DECEMBER 2012
TIME: 3 HOURS
INSTRUCTIONS: Answer questions one and any other two questions

## QUESTION ONE - (30 MARKS)

a) The table below shows the distribution of marks obtained by some students in a statistics examinations.

| Marks (x) | $10-14$ | $15-19$ | $20-24$ | $25-29$ | $30-34$ | $35-39$ | $40-44$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency (f) | 4 | 5 | 8 | 13 | 11 | 6 | 3 |

i. Draw a histogram and frequency polygon using the same axis. (3 Marks)
ii. Draw an ogive curve.
(3 Marks)
iii. Calculate the mean
(2 Marks)
iv. Calculate mode and median
(4 Marks)
v. Calculate the standard deviation
b) If the mean value of the height of 50 people is 165 cm and the standard deviation is 5 cm . How many people have the height.
i. Between 166 and 172 cm .
(2 Marks)
ii. Between 155 and 170
(2 Marks)
iii. Less than 158.
iv. More than 169
(1 Mark)
(1 Mark)
c) The following data present prices for food stuffs between a green grocery shop and an open air market

| Open air <br> market | 22 | 26 | 17 | 20 | 28 | 31 | 23 | 13 | 19 | 25 | 28 | 24 | 27 | 18 | 20 | 14 | 24 | 15 | 19 | 18 | 27 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Green <br> grocery <br> shop | 21 | 29 | 15 | 20 | 26 | 32 | 25 | 14 | 19 | 27 | 27 | 24 | 27 | 20 | 23 | 16 | 26 | 20 | 20 | 17 | 29 |

On the basis of these results use the sign test to investigate if the open air market is cheaper than green grocery shop at $5 \%$ level of significance.
d) The number of births in hundreds of a particular town for 2001 to 2010 were as follows.

| Year | 2001 | 02 | 03 | 04 | 05 | 06 | 07 | 08 | 09 | 2010 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Births | 32 | 24 | 27 | 41 | 34 | 25 | 27 | 26 | 24 | 25 |

Obtain a smoothened value using a five point moving average.
(3 Marks)
e) The following data refer to two variables promotional expenses $\operatorname{Ksh}(10,000)$ and sales in 1000 units, collected in promotional exercise.

| Promotional Expenses in 10000 | Sales in 1000 units |
| :--- | :--- |
| 7 | 12 |
| 10 | 14 |
| 9 | 13 |
| 4 | 5 |
| 11 | 15 |
| 5 | 7 |
| 3 | 4 |

Calculate the correlation coefficient and comment on your answer.
(4 Marks)

## QUESTION TWO - (20 MARKS)

a) Suppose that speeds on a highway are normally distributed with mean $\mu=83.2 \mathrm{Km} / \mathrm{hr}$ and standard deviation $\sigma=9.6 \mathrm{Km} / \mathrm{hr}$. If the police will stop and charge anyone driving in the fastest $1 \%$; what is the fastest speed someone can drive without being stopped?
(6 Marks)
b) The average travel time taken based on a random sample of 10 people working in MUCST to reach the office the office is 40 minutes with a standard deviation of 10 minutes. Establish the $95 \%$ confidence interval for the mean travel time for everyone in MUCST.
(6 Marks)
c) A student magazine at MUCST is conducting a study on the sleeping habits of the students. They collected data for 45 male students and 46 female students and found that male average sleeping hours $\bar{x}_{m}=6.81$ and female average sleeping hours $\bar{x}_{m}=7.37$ with standard deviations $S_{m}=1.22$ and $S_{F}=1.02$. Based on the results, is there any
difference in the mean number of hours that students sleep each night at 5\% level of significance?
(7 Marks)

## QUESTION THREE - (20 MARKS)

a) In a market survey conducted to examine whether choice of a brand is related to the income strata of the consumers, a random sample of 600 consumers revealed the following,

| Income per month | Brand 1 | Brand 2 | Brand 3 | total |
| :--- | :--- | :--- | :--- | :--- |
| Less than Ksh10,000 | 132 | 128 | 50 | 310 |
| Ksh10,000 $-15,000$ | 62 | 60 | 28 | 150 |
| Ksh15,000 $-20,000$ | 30 | 30 | 26 | 86 |
| Above Ksh20,000 | 16 | 22 | 16 | 54 |
| Total | 240 | 240 | 120 | 600 |

Using the $x^{2}$ statistic, test at $5 \%$ level of significance whether the brand preference is associated with the income strata.
(6 Marks)
b) A consumer marketing group desired to examine whether supermarket chains operating in Meru Town differed in their 'out of stock' levels for advertised specials. The group identified the relevant response variable as the percentage of items advertised not in stock. The following data was collected from three supermarket chains in the town.

| Chain 1 | Chain 2 | Chain 3 |
| :--- | :--- | :--- |
| 15 | 10 | 17 |
| 14 | 14 | 12 |
| 20 | 9 | 14 |
| 15 | 10 | 15 |
| 16 | 11 | 12 |

Using ANOVA at 5\% level of significance test whether there are significant differences among the three chains and analyze this situation.
(6 Marks)
c) A shopping mall with a chain of outlets is concerned about its service quality reputation perceived by its customers. The data below shows the perceived service quality with regard to politeness of the staff. The number in each cell of the table is the percentage of people who have said that the staff is polite. Perform the two way ANOVA at $8 \%$ level of significance and draw your inferences about the population means of politeness corresponding to the days as well as the outlets.

| Day/outlet | A | B | C | D | E |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Monday | 79 | 81 | 74 | 77 | 66 |
| Tuesday | 78 | 86 | 89 | 97 | 86 |
| Wednesday | 81 | 87 | 84 | 94 | 82 |


| Thursday | 80 | 83 | 81 | 88 | 83 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Friday | 70 | 74 | 77 | 89 | 68 |

## QUESTION FOUR - (20 MARKS)

a) The data below shows the value for interest rates of Central bank commodities future indexes for a sample of 12 days

| Day | Interest rate | Future index |
| :--- | :--- | :--- |
| 1 | 7.43 | 221 |
| 2 | 7.48 | 222 |
| 3 | 8.0 | 226 |
| 4 | 7.75 | 225 |
| 5 | 7.60 | 224 |
| 6 | 7.63 | 223 |
| 7 | 7.68 | 223 |
| 8 | 7.67 | 226 |
| 9 | 7.59 | 226 |
| 10 | 8.07 | 235 |
| 11 | 8.03 | 233 |
| 12 | 8.00 | 241 |

Calculate the correlation coefficient and comment about the relationship of the two variables.
(6 Marks)
b) A specialist in a government hospital state that the number of full-time employees FTE in a hospital can be estimated by counting the number of beds in the hospital. A survey was carried on 12 hospitals and the following data was obtained;

| Number <br> of Beds | 23 | 29 | 29 | 35 | 42 | 46 | 50 | 54 | 64 | 66 | 76 | 78 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| FTE | 69 | 95 | 102 | 118 | 126 | 125 | 138 | 178 | 156 | 184 | 176 | 225 |

Develop a linear regression model and estimate the number of FTE given 88 number of beds.
c) Suppose the following data set is obtained from prices for the same 15 items at two competing supermarkets A and B

| A | B |
| :--- | :--- |
| 319 | 339 |
| 159 | 149 |
| 209 | 239 |
| 149 | 145 |
| 99 | 99 |
| 245 | 259 |
| 199 | 189 |
| 129 | 139 |
| 149 | 155 |
| 89 | 99 |
| 69 | 75 |
| 112 | 109 |
| 159 | 175 |
| 179 | 189 |
| 53 | 59 |

Based on this data can we conclude that supermarket A is usually cheaper than supermarket B at 5\% level of significance using the sign test method? (5 Marks)
d) A commuter has a choice of driving to work either by a highway (which is often clogged with traffic during morning rush hour) or by back roads which normally are longer. Over the course of several weeks, he tries both routes and times his trip to work. He collected the following data.

| A(Using <br> highway | 34 | 28 | 46 | 42 | 56 | 85 | 48 | 25 | 37 | 49 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| B (back <br> roads) | 43 | 49 | 41 | 55 | 39 | 45 | 65 | 50 | 47 | 51 |

Test using the Rank-sum test if there is any difference in the average time to commute to work at 5\% level of significance.

## QUESTION FIVE - (20 MARKS)

a) The data below shows air pollution by carbon monoxide and nitrogen oxide over a 16 year period.

| Year | $\begin{aligned} & 198 \\ & 5 \end{aligned}$ | 86 | 87 | 88 | 89 | 90 | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | $\begin{array}{\|l} \hline 200 \\ 0 \end{array}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Carb <br> on <br> mono <br> xide | $\begin{aligned} & 176 \\ & .84 \end{aligned}$ | $\begin{aligned} & 173 \\ & .67 \end{aligned}$ | $\begin{aligned} & 172 \\ & .97 \end{aligned}$ | $\begin{aligned} & 174 \\ & .42 \end{aligned}$ | $\begin{aligned} & \hline 160 \\ & .52 \end{aligned}$ | $\begin{aligned} & 154 \\ & .19 \end{aligned}$ | $\begin{aligned} & 147 \\ & .13 \end{aligned}$ | $\begin{aligned} & \hline 14 \\ & 0.9 \end{aligned}$ | $\begin{aligned} & 135 \\ & .90 \end{aligned}$ | $\begin{aligned} & \hline 133 \\ & .56 \end{aligned}$ | $\begin{array}{\|l\|} \hline 126 \\ \hline .78 \end{array}$ | $\begin{aligned} & 128 \\ & .86 \end{aligned}$ | $\begin{aligned} & 117 \\ & .91 \end{aligned}$ | $\begin{aligned} & 115 \\ & .39 \end{aligned}$ | $\begin{aligned} & 114 \\ & .54 \end{aligned}$ | $114$ |
| Nitro gen oxide s | $\begin{aligned} & \hline 25, \\ & 76 \end{aligned}$ | $\begin{aligned} & 25 . \\ & 42 \end{aligned}$ | $\begin{aligned} & 25 . \\ & 58 \end{aligned}$ | $\begin{aligned} & 26 . \\ & 67 \end{aligned}$ | $\begin{aligned} & \hline 25 . \\ & 38 \end{aligned}$ | $\begin{aligned} & 25 . \\ & 53 \end{aligned}$ | $\begin{aligned} & 25 . \\ & 18 \end{aligned}$ | $\begin{aligned} & 25 . \\ & 26 \end{aligned}$ | $\begin{aligned} & 25 . \\ & 36 \end{aligned}$ | $\begin{aligned} & \hline 25 . \\ & 35 \end{aligned}$ | $\begin{array}{\|l\|} \hline 24 . \\ 96 \end{array}$ | $\begin{aligned} & 24 . \\ & 79 \end{aligned}$ | $\begin{aligned} & 24 . \\ & 71 \end{aligned}$ | $\begin{aligned} & 24 . \\ & 35 \end{aligned}$ | $\begin{aligned} & 22 . \\ & 84 \end{aligned}$ | $\begin{aligned} & 22 . \\ & 60 \end{aligned}$ |

i. Calculate 5-point moving average.
(6 Marks)
ii. Plot a time plot and the 5-point moving average on the same axis. (8 Marks)
b) Differentiate between parametric and non-parametric statistic tests.
(2 Marks)
c) State and explain the components of a time series.
(4 Marks)

