



# MERU UNIVERSITY OF SCIENCE AND TECHNOLOGY

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## University Examinations 2013/2014

FIRST YEAR, FIRST SEMESTER EXAMINATION FOR THE DEGREE OF MASTER OF SCIENCE IN APPLIED STATISTICS

### STA 3114: SURVIVAL AND CLINICAL DATA ANALYSIS

DATE: DECEMBER 2013

TIME: 3HOURS

INSTRUCTIONS: Answer question *one* and any other *two* questions

#### QUESTION ONE - (30 MARKS)

- a) i) Define censoring in survival data. (2 Marks)  
ii) Suggest 3 possible reasons for censoring. (3 Marks)
- b) Suppose the time  $T$  is a random variable defined by the survival function  
 $S(t) = e^{-\lambda t}; t > 0, \lambda > 0$
- i. Obtain the probability density function for  $T$ . (3 Marks)  
ii. Find the cumulative distribution function for  $T$ . (2 Marks)  
iii. Find the Harzard function of  $T$ . (2 Marks)  
iv. Find the cumulative Harzard function of  $T$ . (2 Marks)
- c) Consider the data below showing survival times for 21 individuals. The plus sign indicates censored time  
 $6^+, 6, 6, 6, 7, 9^+, 10^+, 13, 16, 17^+, 19^+, 20^+, 22, 23, 25^+, 32^+, 34^+, 35^+$ .  
Obtain the Kaplan Meier estimate of the survival function and plot it. (6 Marks)
- d) Consider the output data below obtained from a Cox proportional Harzards model.

	Coefficients	Se(coefficients)
Treatment 1	-0.3189	0.0669
Treatment 2	0.0172	0.0667

- i. Express the data in a Cox proportional Harzards model and interpret the parameters. (6 Marks)

- ii. Obtain the 95% confidence interval for the Harzard Ratio for both Treatment 1 and Treatment 2. (4 Marks)

**QUESTION TWO (20 MARKS)**

- a) Suppose T is a discrete lifetime that comes from a Geometric distribution.

$$f(t) = \theta(1 - \theta)^t; t = 0,1,2, \dots$$

Obtain

- i. The survival function of T. (3 Marks)
  - ii. The Hazard function of T. (2 Marks)
  - iii. The cumulative Hazard function. (2 Marks)
  - iv. For  $\theta = 2$ , plot both h(t) and H(t) versus time. Comment. (3 Marks)
- b) An electronic firm experiments with two types of light bulbs that they manufacture. The following data shows time in months obtained from the lifespan of the light bulbs.

Group A	1	2	3 <sup>+</sup>	4	4 <sup>+</sup>	7 <sup>+</sup>	8	9	11	15 <sup>+</sup>
Group B	1 <sup>+</sup>	2	2	3	3	4	4	5 <sup>+</sup>	6	7 <sup>+</sup>

- i. Test if the hazard rate in the two groups differs at  $\alpha = 0.05$ . use the Log rank test on  $H_0: h_1(t) = h_2(t)$  versus  $H_1: h_1(t) \neq h_2(t)$  (5 Marks)
- ii. Conduct a test of hypothesis on the hazard rates for the two groups based on the Wilcoxon test. Choose  $\alpha = 0.05$ . Compare results here with those of the Log rank test above. (5 Marks)

**QUESTION THREE (20 MARKS)**

- a) Let T be survival time defined by a survival function

$$S(t) = \frac{t}{1+\lambda^\alpha}; \lambda_1 \alpha = constants$$

- i. Obtain f(t), h(t) and H(t), i.e probability density, hazard and cumulative hazard functions respectively. (4 Marks)
  - ii. Show that the p<sup>th</sup> percentile of the survival time is given by  $t_p = (1 - p)(1 + \lambda^\alpha)$ . (2 Marks)
  - iii. Obtain the median survival time if  $\lambda = \alpha = 0.5$ . (2 Marks)
- b) The remission time in weeks for patients on drug treatment and on control treatment is recorded in weeks. The plus sign indicates censored survival time

Treatment	15	19 <sup>+</sup>	21	22 <sup>+</sup>	30	35
Control	7	8	10 <sup>+</sup>	11	17 <sup>+</sup>	19

- i. Obtain the Kaplan Meier estimate of the survival function for the two groups and plot them on the same axis. Compare the two groups. (6 Marks)

- ii. Conduct a Logrank test of hypothesis ( $\alpha = 0.05$ ) to compare the two groups. Is the drug effective? (6 Marks)

**QUESTION FOUR (20 MARKS)**

- a) Using the Delta method, prove that;  
 “If a random variable  $Y \sim N(\mu, \sigma^2)$ , then a function of Y given by  $g(Y)$  is approximately normal mean  $g(\mu)$  and variance  $[g'(\mu)]^2 \sigma^2$ ”.
- b) The Kaplan Meier estimator of a function is given by

$$\hat{S}(t) = \prod_{t_j \leq t} \frac{r_j - d_j}{r_j}; r_j = \text{risk set}, d_j = \text{number of deaths at } t_j$$

If  $\hat{P}_j \sim N\left(p_j, p_j \frac{(1-p_j)}{r_j}\right), E\left(\hat{S}(t) = S(t)\right)$ , show that

$$\text{var}\left(\hat{S}(t_j)\right) = [S(t)]^2 \sum_{t_j \leq t} \frac{d_j}{r_j(r_j - d_j)}$$

**QUESTION FIVE (20 MARKS)**

Conduct a multivariate Log rank test of hypothesis to compare the survival in the three groups below. choose  $\alpha = 0.05$ .

Group 1	20	21	23	24	24	26	26	27	28	30
Group 2	26	28	29	29	29	30	31	31	32	-
Group 3	31	32	34	35	36	38	38	39	-	-

(20 Marks)