

University Examinations 2012/2013

FIRST YEAR, THIRD SEMESTER EXAMINATION FOR MASTER OF SCIENCE IN APPLIED MATHEMATICS

SMA 3137: NUMERICAL ANALYSIS II

DATE: DECEMBER 2012

TIME: 3HOURS

INSTRUCTIONS: Answer questions **one** and any other **two** questions

QUESTION ONE - (30 MARKS)

	Approximate the singular integral $\int_0^\infty e^{-x^2 - \frac{1}{x^2}} dx$	(9 Marks)
b)	Find the value of the integral $\int_{2}^{3} \frac{\cos 2x}{1+\sin x} dx$, Using the Gauss-Legendre 3-	point formula
	giving your answer correct to 6 decimal places.	(7 Marks)
c)	Given the differential equation $\frac{dy}{dt} = t - y^2$, $y(0) = 1$, compute $y(0.1)$,	y(0.2)and
	y(0.3) using the modified Euler method with $h = 0.1$	(6 Marks)
d)	Use the finite difference method to solve the boundary value problem	
	$\frac{d^2y}{dx^2} = y,$	
	y(0) = 0, y(2) = 3.627. Use h = 0.5	(8 Marks)

QUESTION TWO – (20 MARKS)

- a) Approximate the integral $\int_0^1 e^{x^2} dx$ Using Newton – Cotes method corresponding to n = 3 (11 Marks)
- b) Use Romberg integration method to find an approximation to the integral

$\int_0^3 f(x) dx$ from the following functional data:

x	0.00	0.75	1.50	2.25	3.00
f(x)	1.0000	0.47235	0.22313	0.10540	0.04979

(9 Marks)

QUESTION THREE – (20 MARKS)

- a) Estimate $\int_{0}^{0.5} \int_{0}^{0.5} \frac{\sin(xy)}{1+xy} dx dy$ Using Simpson's rule for double integrals with both steps sizes = 0.25 (10 Marks)
- b) Using Schmidt explicit formula solve the equation $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$ Subject to the conditions $u(x, 0) = \sin \pi x$, $0 \le x \le 1$, u(0, t) = u(1, t) = 0Carry out computation for two levels taking $h = \frac{1}{3}$, $k = \frac{1}{36}$. (10 Marks)

QUESTION FOUR - (20 MARKS)

Use the ABAM and Runge-Kutta methods to approximate x(2) for the initial value problem

$$\frac{dx}{dt} = 5t - 2x, x(0) = 1 \text{ Using step size } h = 0.5 \text{ correct to 5 d.p.}$$
(20 Marks)