



SOUTH EASTERN KENYA UNIVERSITY

UNIVERSITY EXAMINATIONS 2016/2017

FIRST SEMESTER EXAMINATION FOR THE DEGREE OF BACHELOR OF SCIENCE IN (PHYSICS/ELECTRONICS/GEOLOGY/METEOROLOGY) AND BACHELOR OF EDUCATION (SCIENCE)

SPH 203: STRUCTURE AND PROPERTIES OF MATTER

8TH DECEMBER, 2016

TIME: 1.30-3.30 P.M

INSTRUCTIONS TO CANDIDATES

- This paper consists of **FIVE (5)** questions.
- Answer question **ONE** and any other **TWO** questions.
- Question **ONE** carries 30 marks while the other **TWO** questions carry 20 marks each.
- The following constants may be necessary

Molar gas constant, $R = 8.3\text{Jmol}^{-1}\text{K}^{-1}$

Avogadro's constant $N_A = 6.0 \times 10^{23}\text{mol}^{-1}$

Young's modulus of steel = $2.0 \times 10^{11}\text{ Pa}$,

Linear expansivity of steel = $1.6 \times 10^{-7}\text{ }^\circ\text{C}^{-1}$

Volume of unit cell for aluminium $V_u = 8.99 \times 10^{-29}\text{m}^3$

QUESTION ONE (COMPULSORY) (30MARKS)

- a) (i) Differentiate surface tension and free surface energy (2marks)

- (ii) A soap bubble was slowly enlarged from a radius of 6 cm to a radius of 9 cm. the amount of work necessary for the enlargement was 20×10^{-4} Joules. Calculate the surface tension of the soap bubble (3marks)
- b) (i) Bernoulli's equation states the consequences of the principle that work done on a fluid as it flows from one place to another is equal to the change in its mechanical energy. State the four conditions under which this principle is valid (4marks)
- (ii) A horizontal pipe of cross sectional area 15 cm^2 carries water from one place to another. At the second point, the pressure difference is observed to be 200 Nm^{-2} . Determine the volume flux. (5marks)
- c) A 20 m length of continuous steel railway line of cross sectional area $8.0 \times 10^{-3} \text{ m}^2$ is welded into place after heating to a uniform temperature of 40°C . Taking Young's modulus for steel to be $2.0 \times 10^{11} \text{ Pa}$, its linear expansivity to be $12 \times 10^{-6} \text{ K}^{-1}$, its density to be 7800 kgm^{-3} and its specific capacity to be $500 \text{ Jkg}^{-1} \text{ K}^{-1}$, calculate, for normal operating conditions at 15°C ;
- The tensile strain (2marks)
 - The tensile stress (3marks)
 - The elastic strain energy in the rail (3marks)
- d) A mole of an ideal gas at 300 K is subjected to a pressure of 10^5 Pa and its volume is 0.0025 m^3 . Calculate:
- The molar gas constant R (2marks)
 - The Boltzmann constant k (2marks)
 - The average translational kinetic energy of a molecule of the gas (4 marks)
- ($N_A = 6.0 \times 10^{23} \text{ mole}^{-1}$)

QUESTION TWO (20MARKS)

- a)
- i. Define a polymer. (1mark)
 - ii. Distinguish between a thermosetting and thermoplastic polymers giving an example in each case (3marks)
 - iii. For ionic crystals, show that the main contribution to the binding energy of ionic crystals is electrostatic and is given by the Madelung energy expressed by

$$U_{R_0} = -\frac{9}{10} \left[N_0 \frac{Q^2}{4\pi\epsilon_0 R_0} \alpha \right] \quad (10marks)$$

- b) i. Differentiate between density and packing fraction as used in crystal structure (2marks)
- ii. Calculate the packing fraction for the Body Centered Cubic (BCC) crystal structure of sodium. Take lattice parameter 'a' as 4.22Å (4marks)

QUESTION THREE (20MARKS)

- a) Aluminium has a density of 2699kgm⁻³ and its atomic weight is 26.97
- i. determine how many moles of aluminium are contained in 1 m³ of the solid (3marks)
 - ii. calculate the number of atoms contained in 1m³ (2marks)
 - iii. determine the length of the unit cube for this FCC metal (5marks)
 - iv. calculate the atomic radius of aluminium atom (3marks)
 - v. determine the weight of a single atom of aluminium (2marks)

- (b) Consider a clean narrow tube of internal radius R held vertically and lowered into water. Show that the surface tension is given by

$$\gamma = \frac{R\rho g}{2\cos\theta} \left(h + \frac{R}{3} \right) \quad (5\text{marks})$$

- (c) A steel rod of length 0.60m and cross sectional area $2.5 \times 10^{-5} \text{ m}^2$ at 100°C is clamped so that when it cools it is unable to contract. Find the tension in the rod when it has cooled to 20°C . (5marks)

QUESTION FOUR (20 MARKS)

- a)
- Derive Poiseuille's formula $V = \frac{\pi P a^4}{8\eta L}$ for a fluid through a narrow tube
(Symbols have their usual meaning) (10marks)
 - State the assumptions made in the above derivation (2marks)
- b) An empty vessel which is open at the top has a horizontal capillary tube of length 20 cm and internal radius 1.0 mm protruding from one of its side walls immediately above the base. Water flows into the vessel at a constant rate of $1.5 \text{ cm}^3\text{s}^{-1}$. Determine the depth at which the water level will stop rising. Assume the flow is steady, the coefficient of viscosity for water = $1.0 \times 10^{-3} \text{ Nsm}^{-2}$, density of water = $1.0 \times 10^3 \text{ kgm}^{-3}$ and acceleration due to gravity = 10 ms^{-2} (8marks)

QUESTION FIVE (20MARKS)

- a) Air is contained in a cylinder by a frictionless gas-tight piston. Find the work done by the gas as it expands from a volume of 0.015 m^3 to a volume of 0.027 m^3 at a constant pressure of $2.0 \times 10^5 \text{ Pa}$. (5marks)

- b) Find the final pressure if, starting from the same initial conditions as in (a), and expanding by the same amount, the change occurs
- i. Isothermally
 - ii. Adiabatically (γ for air = 1.40) (5marks)
- c) A steel pressure vessel of volume $2.2 \times 10^{-2} \text{ m}^3$ contains $4.0 \times 10^{-2} \text{ kg}$ of a gas at a pressure of $1.0 \times 10^5 \text{ Pa}$ and temperature 300 K. An explosion suddenly releases $6.48 \times 10^4 \text{ J}$ of energy, which raises the pressure instantaneously to $1.0 \times 10^6 \text{ Pa}$. assuming no loss of heat to the vessel and ideal gas behavior, calculate:
- i. The maximum temperature attained (3marks)
 - ii. The two principal specific heat capacities of the gas (4marks)
 - iii. Determine the velocity of sound in this gas at a temperature of 300 K (3marks)