



MERU UNIVERSITY OF SCIENCE AND TECHNOLOGY

P.O. Box 972-60200 - Meru-Kenya.

Tel: 020-2069349, 061-2309217. 064-30320 Cell phone: +254 712524293, +254 789151411

Fax: 064-30321

Website: www.mucst.ac.ke Email: info@mucst.ac.ke

University Examinations 2014/2015

EXAMINATION FOR CERTIFICATE IN BRIDGING MATHEMATICS

SMB 0103: BASIC CALCULUS AND MATRICES

DATE: DECEMBER 2014

TIME: 1 $\frac{1}{2}$ HOURS

INSTRUCTIONS:

QUESTION ONE

- a) Find the solution of the system by Cramer's rule (4 marks)

$$x+y=5$$

$$3x-2y=0$$

- b) Estimate the area enclosed by the curve $y=\frac{1}{2}x^2+1$, $x=0$, $x=4$ and the x-axis using the mid-ordinate rule (4 marks)

- c) Evaluate

$$\lim_{x \rightarrow 3} \left[\frac{x^2 - 9}{x - 3} \right] \quad (4 \text{ marks})$$

- d) Given the $A = \{1, 3, 5, 7\}$, list the members of the following sets.

(i) $(x^3 : x \in A)$ (1 mark)

(ii) $(2x + 3 : x \in A)$ (1 mark)

- e) Find the derivatives $\frac{x^3}{3x+1}$ (4 marks)

- f) Given the equation of the curve $y=x^2-1$, at point (2,3). Find the equation of

- (i) tangent (3 marks)
(ii) normal (3 marks)

g) Find the inverse of $\begin{bmatrix} 3 & 2 \\ 0 & 1 \end{bmatrix}$ (3 marks)

h) Evaluate $\int_2^3 (x^2 + 1) dx$ (3 marks)

QUESTION TWO

a) The displacement s metres of a particle after t seconds is given by $s=40t^3-t^2+3t+3$. Find its velocity and acceleration when $t=2$. (6 marks)

b) Use the matrix method to solve (4 marks)

$$5x+3y=7$$

$$2x+y=5$$

QUESTION THREE

a) Evaluate $\lim_{x \rightarrow 4} \left[\frac{x^2 + 8x + 16}{x + 4} \right]$ (4 marks)

b) Given that $A = \{-1, 0, 1, 2, 3\}$ list the members of the following sets (4 marks)

(i) $\{x^2 : x \in A\}$

(ii) $\left\{ \frac{1}{x} : x \in A \right\}$

(iii) $\{2x : x \in A\}$

(iv) $\{4x + 1 : x \in A\}$

c) Find the gradient of $y=x^2$ at $x=1$ (2 marks)

QUESTION FOUR

a) Use the trapezium rule to estimate the area under the curve $y=2x^2+6$ the $x=1$ and $x=5$ and the x -axis. Use 8 strips (5 marks)

b) The demand for the product of a firm varies with the price that the firm charges for the product. The firm estimates that the annual total revenue R as the function of the price P is given by $R=f(p)=100p^2+100p$. Determine the price, which should be charged in order to maximise total revenue. (5 marks)

QUESTION FIVE

a) Estimate the area enclosed by the curve $y=\frac{1}{2}x^2 + 3$, $x=0$, $x=5$ and the x -axis using the mid-ordinate rule. (6 marks)

b) Given that A is the set of odd numbers less than 20 and B is the set of prime number less than 20, list the members of (4 marks)

(i) A

(ii) B

(iii) $A \cap B$

(iv) $A \cup B$

QUESTION SIX

- a) Solve the equation using the determinant method (4 marks)

$$3x+4y=18$$

$$x+2y=8$$

- b) Estimate the area enclosed by the curve $y=\frac{1}{2}x^2 + 1$, $x=0$, $x=4$ and the x-axis using the trapezium rule (6 marks)