

**University Examinations 2012/2013**

**THIRD YEAR, SECOND SEMESTER, EXAMINATION FOR THE DEGREE OF BACHELOR  
OF SCIENCE IN COMPUTER TECHNOLOGY**

**BCT 2310: AUTOMATA THEORY**

**DATE: DECEMBER 2012**

**TIME: 2 HOURS**

**INSTRUCTIONS:** Answer question *one* and any other *two* questions

**QUESTION ONE – 30 MARKS**

- a. Discuss two ways of accepting an input string by pushdown automata. (4 Marks)
- b. Define the following terms and give an example of each. (2 Marks)
  - i. Alphabets
  - ii. Strings
- c. Draw a (state) transition diagram of the DFA below. (3 Marks)
  
  
  
  
  
  
  
  
  
  
- d. What is decidability and undecidability of problems? (4 Marks)
- e. What is Turing test? (2 Marks)
- f. What is an accepting or rejecting state of a finite automata? (2 Marks)
- g. Outline the importance of studying automata theory. (3 Marks)
- h. Give an application of context free grammars. (4 Marks)
- i. Discuss context sensitive grammars and context free grammars. (4 Marks)
- j. Let  $A = \{a, b, c\}$ ,  $B = \{b, d, c\}$ . Find (2 Marks)
  - i.  $A \cap B$
  - ii.  $A \cup B$

## QUESTION TWO – 20 MARKS

a. Convert the following NFA to DFA

(10 Marks)

b. Describe the three properties of closure of regular expressions.

(10 Marks)

## QUESTION THREE – 20 MARKS

a. Give DFA for recognizing the language of all binary strings ending in 0110.

(4 Marks)

b. With the transition table below, produce a DFA

(12 Marks)

States	a	b	c
0	0	0	0
1	2	0	0
2	0	3	0
3	0	0	4
4	2	0	4

$q_0$  is 0 and  $F = \{3, 4\}$

c. Find a regular expression corresponding to the language of all strings over the alphabet  $\{a, b\}$  that contain exactly three a's.

(4 Marks)

#### QUESTION FOUR – 20 MARKS

- a. Describe a deterministic one-tape turing machine and how it works. (4 Marks)
- b. Describe the Chomsky normal form. (2 Marks)
- c. Calculate how many words there are in the following languages. List three elements in each of them. Which language contains  $\varepsilon$ ? (4 Marks)

$\Sigma^*$ , where  $\Sigma = \{a, b, c\}$

$w \in \Sigma^* \mid |w| = 4\}$ ,

where  $\Sigma = \{a, b\}$

$\{w \in \Sigma^* \mid |w| = 4\}$ , where  $\Sigma = \{a, b\}$

$\{a^n \mid n \text{ is prime}\}$

- d. Find regular expressions for the following NFAs (10 Marks)

#### QUESTION FIVE – 20 MARKS

- a. Discuss the four characteristics of finite automata. You may use diagrams where possible. (8 Marks)
- b. Discuss the following: (4 Marks)
- c. What is decidability and undecidability of problems? (2 Marks)
- d. Given the following:

$\Sigma = \{a\}$

Productions:

$\rightarrow S \quad aS$

$\rightarrow S \quad \Lambda$

Trace the execution of applying rule 1 three times and rule 2 once.

(4 Marks)