

UNIVERSITY

## UNIVERSITY EXAMINATIONS

## EXAMINATION FOR THE AWARD OF DEGREE OF BACHELOR OF

## MATH 141: INTRODUCTION STASTICS

STREAMS:
TIME: 2 HOURS

DAY/DATE : TUESDAY 17/04/2018
2.30 P.M - 4.30 P.M

INSTRUCTIONS:

- Answer question one and any other two questions
- All workings must be shown clearly
(i) (a) State with examples the differences between ;
(i) Descriptive statistics and a data set.
(ii) Marginal and conditional probability
(iii) Event and a sample space.
(b) Calculate the rank correlation coefficient for the following data on two tests.

| Test | x | 84 | 77 | 62 | 54 | 93 | 86 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Test | Y | 73 | 85 | 53 | 58 | 84 | 90 |

Comment on the correlation between X and Y .
(c) Define probability and state two laws of probability.
(d) Write down three questions as a questionnaire about usage of a tooth paste. Your respondents are from the rural areas.
(e) Find the standard deviation of the following data.
$\begin{array}{lllll}1330 & 1305 & 1310 & 1320 & 1315\end{array}$
(f) Differentiate between observation and interview as methods of data collection.
[5marks]
(g) Kokopey company has tendered two independent contracts. It estimates that it has a probability of 0.5 for obtaining contrast A and 0.3 for obtaining contract B. Find the probability that the company obtains.
(i) At most one contract
(ii) Contract A given contract B

Are the contracts independent?
2. (a) Explain briefly the methods of least squares in regression analysis. [5marks]
(b) The following are weights and heights of a group of seven students taking probability and statistics course.

| Weight | X | 56 | 60 | 62 | 65 | 70 | 80 | 90 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Height | Y | 138 | 148 | 150 | 156 | 153 | 160 | 173 |

## Required :

(i) Fit a least squares line to the data.
(ii) Estimate the height when the weight is 58 kg .
(iii) Obtained the correlation coefficient.
(c) The following frequency distribution has a mean of 34.66 and total frequency of 125.

| Class | $0-9$ | $10-19$ | $20-29$ | $30-39$ | $40-49$ | $50-59$ | $60-69$ | $70-79$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| frequency | 15 | 15 | X | 22 | 25 | Y | 5 | 10 |

3. (a) The data below represent scores of two basket ball teams.

| Kenya | 30 | 41 | 22 | 54 | 50 | 39 | 47 | 43 | 57 | 28 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Rwanda | 29 | 40 | 38 | 56 | 47 | 59 | 58 | 58 | 38 | 56 |

## Required :

Create a "back to back" stem and leaf plot
[4marks]
(b) Two fair dice are tossed and the following events are defined.
$\mathrm{A}=\{$ sum of the numbers showing is odd $\}$
$B=\{$ sum of the numbers showing is $9,11 \& 12\}$
Are the events A \&B independent? Why? Show your working.
[4marks]
(c) Two events E and F are such that $\mathrm{P}(\mathrm{E})=0.7, \mathrm{P}(\mathrm{F})=0.6$ and $\mathrm{P}(\mathrm{E} \cup F)=0.8$

Find (i) $\mathrm{P}(\mathrm{E} \cap F)$
[2marks]
(ii) $\mathrm{P}\left(E^{c} \cap F\right)$
[2marks]
(iii) $\mathrm{P}\left(E^{c} \cap F^{c}\right)$
[2marks]
(d) The blood type distribution in the united states is as follows ;

$$
\begin{aligned}
& \text { Type A }=40 \% \\
& \text { Type B }=9 \% \\
& \text { Type AB }=4 \% \\
& \text { Type } 0=46 \%
\end{aligned}
$$

It is estimated that during world war II $4 \%$ of inductees with type 0 blood were typed as having type A, $88 \%$ of those with type A were correctly typed, $4 \%$ with type B blood were typed as A and $10 \%$ with type AB were type as A. A soldier was wounded and brought to surgery. He was typed as having type A blood. What is the probability that this his true blood type?
[6marks]
4. (a) A class consists of 24 boys and 26 girls. The mean score of the boys in a certain subject is 68 while mean score of the whole class is 70.08 . Find the mean score of the girls in the class.
[3marks]
(b) The table below shows the distribution of marks scored by 50 candidates in an examination.

| Mark | Number of students |
| :--- | :--- |
| $0-10$ | 3 |
| $10-20$ | 7 |
| $20-30$ | 10 |
| $30-40$ | 14 |
| $40-50$ | 11 |
| $50-60$ | 5 |
| $60-70$ | 2 |

## Calculate ;

(i) Mean absolute deviation
[7marks]
(ii) Standard deviation
(iii) Coefficient of variation
(iv) Mode
[6marks]
[2marks]
[5marks]
5. The data below shows the weight to the nearest cm of height of 100 seedlings in a nursery.

| 33 | 68 | 31 | 36 | 16 | 34 | 56 | 38 | 43 | 52 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 24 | 49 | 76 | 52 | 36 | 85 | 4 | 44 | 56 | 19 |
| 46 | 38 | 7 | 34 | 65 | 44 | 95 | 63 | 30 | 22 |
| 11 | 29 | 48 | 50 | 27 | 31 | 24 | 29 | 14 | 39 |
| 43 | 86 | 55 | 15 | 69 | 43 | 52 | 17 | 45 | 65 |
| 37 | 42 | 46 | 67 | 32 | 58 | 34 | 89 | 47 | 28 |
| 24 | 16 | 32 | 31 | 6 | 45 | 28 | 67 | 29 | 52 |
| 35 | 37 | 43 | 63 | 56 | 25 | 48 | 55 | 78 | 49 |
| 73 | 48 | 59 | 18 | 38 | 77 | 35 | 26 | 33 | 31 |
| 26 | 40 | 38 | 25 | 26 | 39 | 72 | 13 | 8 | 24 |

(a) Using the class 1-10, 11-20 etc construct a frequency distribution table for the data. [5marks]
(b) Draw a frequency distribution curve (ogive) on the graph paper provided. [5marks]
(c) Use the curve construct above to determine.
(i) Median
(ii) $1^{\text {st }}$ quartile and $3^{\text {rd }}$ quartile
[2marks]
(iii) $6^{\text {th }}$ decile [2marks]
(iv) The number of seedlings to be transplanted if any seedling having height of 35 cm and above has to be transplanted.

