## CHUKA



UNIVERSITY

## UNIVERSITY EXAMINATIONS

## EXAMINATION FOR THE AWARD OF DEGREE OF DIPLOMA IN TOURISM AND HOTEL MANAGEMENT

## MATH 0121: INTRODUCTORY MATHEMATICS

STREAMS: DIP (DTHM)
TIME: 2 HOURS
DAY/DATE: THURSDAY 09/08/2018
8.30 AM - 10.30 AM

INSTRUCTIONS:
ANSWER QUESTION ONE AND ANY OTHER TWO QUESTIONS
QUESTION ONE
a) State the properties of real numbers in the equations below
i) $2=2 \times 1$
ii) $8(3+2 y)=24+16 y$
iii) $(2+3)+8=2+(3+8)$
iv) $2(12)=2(12)$
b) $\quad$ Given $U=\{2,4,6,8,10,12,14,16,18,20\}$

$$
\begin{aligned}
& A=\{6,10,14\} \\
& B=\{8,14,18,20\}
\end{aligned}
$$

Find
i) $\quad \mathrm{A}^{\mathrm{c}}$
ii) $\quad B^{c}$
iii) $\quad(\mathrm{A} \cap B)^{\mathrm{c}}$
marks]
c) Given $f(x)=4 x+3$

$$
\begin{aligned}
& g(x)=-7 x \quad-x^{2}+5 \\
& h(x)=3 x^{3}-6 x^{2}+7
\end{aligned}
$$

Find
i) $\quad f(x)+g(x)$
ii) $\quad 2 g(x)-h(x)$
iii) $\quad g(x) \times h(x)$
[4marks]
d) A committee of 5 men and 4 women is to be chosen from 8 men and 6 women. In how many ways can this be done
e) Simplify $\frac{6+4 i}{2-i}$
marks]
f) Show that $\frac{\tan \theta}{\sin \theta}=\sec \theta$
marks]
g) Classify the following numbers
i) $\quad-2.2222$
ii) 3
iii) $\quad \sqrt{ } 5$
iv) $\frac{22}{7}$
marks]
h) Find the quotient and the remainder when $\mathrm{x}^{3}-\mathrm{x}^{2}-\mathrm{x}+1$ is divided by $\mathrm{x}-1$

## QUESTION TWO

a) Expand and simplify the binomial expansion:(2 $\left.\frac{-1}{2} y \quad\right)^{5}$ marks]
b) How many arrangements are there for the letters of the word PREUNIVERSITY [4 marks]
c) Solve for n in ${ }^{\mathrm{n}} \mathrm{C}_{2}=28$
[5 marks]
d) Write out the following series and evaluate them
i) $\quad \sum_{i=1}^{6} i^{2}$
ii) $\quad \sum_{i=1}^{6} \frac{1}{i(1+i)}$
[6 marks]

## QUESTION THREE

a) (i) Complete the table below
[4 marks]
$\left.\begin{array}{|c|l|l|l|l|l|l|l|l|l|l|l|l|l|}\hline \theta & 0 & 30 & 60 & 90 & \begin{array}{l}12 \\ 0\end{array} & \begin{array}{l}15 \\ 0\end{array} & \begin{array}{l}18 \\ 0\end{array} & 210 & 240 & 270 & 300 & 330 & 360 \\ \hline \begin{array}{c}\tan \\ \frac{1}{2} x\end{array} & & & & & & & & & \begin{array}{l}- \\ 1.73\end{array} & & & & \\ \hline 2 \cos x & & & & & & & & & - \\ 1.00\end{array}\right)$
i) Using the grid provided draw the graph of $y=\tan \frac{1}{2} x$ and $y=2 \cos x$ [6marks]
ii) Use your graph to solve

$$
\tan \frac{1}{2} x=2 \cos x
$$

[2 marks]
$2 \cos x-1.5=0$
b) In how many ways can 4 boys and 2 girls be seated in 9 rows such that
i) The boys and girls can sit anywhere
ii) The two girls must sit together
iii) The two girls must be separated
c) Define a fallacy and a tautology

## QUESTION FOUR

a) Given that $f(x)=4 x^{2}-5$ and $g(x)=x+3$, find

## 3

i) $\quad$ fog $i$ )
ii) $g \circ f(3)$
iii) $\operatorname{gog}(x)$
iv) $f \circ f(x)$
b) Show that $(P \vee Q)=P \Lambda Q$
c) In an AP of 25 terms, the $4^{\text {th }}$ term is $4,22^{\text {nd }}$ term is 5 . Find the sum of the AP
[5marks)
d) In a class of 40 students 30 of them passed in physics and 28 passed English. How many students passed both subjects? Illustrate your answer on a Venn diagram.
[5marks]

## QUESTION FIVE

a) Prove analytically that $(A \cup B) U C=A \cup(B \cup C)$
[5 marks]
b) The second term of a GP is 2 and the fourth term is 8 . Find the possible values of the common ratio and the corresponding first terms
[5marks]
c) A school committee of nine members is to be formed 8 parents and 6 teachers and the principal. In how many ways can the committee be formed in order to include
i) The principal
ii) The principal and 5 parents
[6 marks]
d) $\operatorname{Let} g(x)=2 x^{3}+3 x^{2}-2 x+1$,

Find
g (1)
$\mathrm{g}\left(\mathrm{x}^{2}\right)$
$g(2)+g(-1)$

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