



UNIVERSITY EXAMINATIONS: 2020/2021
FINAL EXAMINATION FOR THE DEGREE OF BACHELOR OF
COMMERCE

STA 2101: BUSINESS STATISTICS II

CMS 301-F: ADVANCED BUSINESS STATISTICS

OPEN BOOK: WEEKEND AND DISTANCE LEARNING

DATE: AUGUST 2020

TIME: 3 HOURS

INSTRUCTIONS: Answer *BOTH* Questions

QUESTION 1 (25 MARKS)

a.) The Mental Development Index (MDI) of the Bayley Scales of Infant Development is a standardized measure used in studies with high-risk infants. It has approximately a normal distribution with a mean of 100 and a standard deviation of 16. Find and interpret the semi-interquartile range.

[4 marks]

b.) Five students- the females Ann, Betty and Catherine; and the males Douglas, and Edward—are rated equally qualified for admission to KCA University, ahead of other applicants. However, all but three positions have been filled for the new class. The Admissions Committee can admit only three more students, so it decides to randomly select three of these five candidates. For this strategy, let X = number of females admitted.

i.) Construct the probability distribution for X . [3 marks]

ii.) Construct the sampling distribution of the sample proportion of the students selected who are female. [4 marks]

c.) A certain survey contained this as one of the key questions: “What do you think is the ideal number of children for a family to have?” The 497 females who responded had a median of 2, mean of 3.02, and standard deviation of 1.81.

- i.) Find and interpret the margin of error in this estimation using $\alpha = 0.05$. [2 marks]
- ii.) The 95% confidence interval is (2.9, 3.2). Interpret. [2 mark]
- iii.) Is it plausible that the population mean = 2.0? Explain. [2 marks]
- iv.) If the estimate should be correct to within 0.10 with a probability of 0.95, how large a sample should be selected? [3 marks]

d.) A study seeks to estimate the mean monthly family income for families living in government-owned houses in Nairobi. For a random sample of 30 families, the monthly incomes (in thousands of shillings) are given below:

133	140	127	150	133	114	128	142	123	172	146	110
135	136	158	120	189	106	144	134	161	143	170	120
142	150	174	109	162	129						

- i.) Based on a descriptive graphic, what do you predict about the shape of the population distribution? [2 marks]
- ii.) Find and interpret point estimates of the population mean and standard deviation. [4 marks]
- iii.) Construct and interpret a 95% confidence interval for the population mean. [3 marks]

QUESTION 2 (25 MARKS)

a.) In making a decision in a test, a researcher worries about the possibility of rejecting H_0 when it is actually true. Explain how to control the probability of this type of error.

[3
marks]

- b.) In a certain exit poll of 1330 registered voters in the 2016 senatorial election, let Y = number in exit poll who voted for candidate A.
- i.) Explain why this scenario would seem to satisfy the conditions needed to use the binomial distribution. [2 marks]
 - ii.) If the population proportion voting for candidate A had been 0.50, find the mean and standard deviation of the probability distribution of Y . [2 marks]
 - iii.) For (ii), using the normal distribution approximation, give an interval in which Y would almost certainly fall. [2 marks]
 - iv.) Now, actually the exit poll had $Y = 723$. Explain how you could make an inference about whether the population proportion is above or below 0.50. [3 marks]
- c.) In a sentence or two say what it means to have mean chart out of control whereas the range chart for the same process is within control. In a quality control process of your choice, list any three possible causes of such a situation. [4 marks]
- d.) A random sample of the following two variables was obtained:

x (Independent)	1	2	3	4	5
y (Dependent)	4	2	5	8	9

- i.) Construct a scatter plot of these data. Describe the relationship between X and Y . [1 marks]
- ii.) Calculate the sum of squares error for the following equations:
 1. $\hat{y} = 0.8 + 1.60x$
 2. $\hat{y} = 1 + 1.50x$ [2 marks]
- iii.) Which of these equations provides the “best” fit of these data? Describe the criterion you used to determine “best” fit. [2 marks]

Determine the regression line that minimizes the sum of squares error for the data

a

t - Table with right tail probabilities

α	0.40	0.25	0.10	0.05	0.025	0.01	0.005	0.0005
1	0.324920	1.000000	3.077684	6.313752	12.70620	31.82052	63.65674	636.6192

2	0.288675	0.816497	1.885618	2.919986	4.30265	6.96456	9.92484	31.5991
3	0.276671	0.764892	1.637744	2.353363	3.18245	4.54070	5.84091	12.9240
4	0.270722	0.740697	1.533206	2.131847	2.77645	3.74695	4.60409	8.6103
5	0.267181	0.726687	1.475884	2.015048	2.57058	3.36493	4.03214	6.8688
6	0.264835	0.717558	1.439756	1.943180	2.44691	3.14267	3.70743	5.9588
7	0.263167	0.711142	1.414924	1.894579	2.36462	2.99795	3.49948	5.4079
8	0.261921	0.706387	1.396815	1.859548	2.30600	2.89646	3.35539	5.0413
9	0.260955	0.702722	1.383029	1.833113	2.26216	2.82144	3.24984	4.7809
10	0.260185	0.699812	1.372184	1.812461	2.22814	2.76377	3.16927	4.5869
11	0.259556	0.697445	1.363430	1.795885	2.20099	2.71808	3.10581	4.4370
12	0.259033	0.695483	1.356217	1.782288	2.17881	2.68100	3.05454	4.3178
13	0.258591	0.693829	1.350171	1.770933	2.16037	2.65031	3.01228	4.2208
14	0.258213	0.692417	1.345030	1.761310	2.14479	2.62449	2.97684	4.1405
15	0.257885	0.691197	1.340606	1.753050	2.13145	2.60248	2.94671	4.0728
16	0.257599	0.690132	1.336757	1.745884	2.11991	2.58349	2.92078	4.0150
17	0.257347	0.689195	1.333379	1.739607	2.10982	2.56693	2.89823	3.9651
18	0.257123	0.688364	1.330391	1.734064	2.10092	2.55238	2.87844	3.9216
19	0.256923	0.687621	1.327728	1.729133	2.09302	2.53948	2.86093	3.8834
20	0.256743	0.686954	1.325341	1.724718	2.08596	2.52798	2.84534	3.8495
21	0.256580	0.686352	1.323188	1.720743	2.07961	2.51765	2.83136	3.8193
22	0.256432	0.685805	1.321237	1.717144	2.07387	2.50832	2.81876	3.7921
23	0.256297	0.685306	1.319460	1.713872	2.06866	2.49987	2.80734	3.7676
24	0.256173	0.684850	1.317836	1.710882	2.06390	2.49216	2.79694	3.7454
25	0.256060	0.684430	1.316345	1.708141	2.05954	2.48511	2.78744	3.7251
26	0.255955	0.684043	1.314972	1.705618	2.05553	2.47863	2.77871	3.7066
27	0.255858	0.683685	1.313703	1.703288	2.05183	2.47266	2.77068	3.6896
28	0.255768	0.683353	1.312527	1.701131	2.04841	2.46714	2.76326	3.6739
29	0.255684	0.683044	1.311434	1.699127	2.04523	2.46202	2.75639	3.6594
30	0.255605	0.682756	1.310415	1.697261	2.04227	2.45726	2.75000	3.6460
inf	0.253347	0.674490	1.281552	1.644854	1.95996	2.32635	2.57583	3.2905

Area between 0 and z										
	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.0000	0.0040	0.0080	0.0120	0.0160	0.0199	0.0239	0.0279	0.0319	0.0359
0.1	0.0398	0.0438	0.0478	0.0517	0.0557	0.0596	0.0636	0.0675	0.0714	0.0753

0.2	0.0793	0.0832	0.0871	0.0910	0.0948	0.0987	0.1026	0.1064	0.1103	0.1141
0.3	0.1179	0.1217	0.1255	0.1293	0.1331	0.1368	0.1406	0.1443	0.1480	0.1517
0.4	0.1554	0.1591	0.1628	0.1664	0.1700	0.1736	0.1772	0.1808	0.1844	0.1879
0.5	0.1915	0.1950	0.1985	0.2019	0.2054	0.2088	0.2123	0.2157	0.2190	0.2224
0.6	0.2257	0.2291	0.2324	0.2357	0.2389	0.2422	0.2454	0.2486	0.2517	0.2549
0.7	0.2580	0.2611	0.2642	0.2673	0.2704	0.2734	0.2764	0.2794	0.2823	0.2852
0.8	0.2881	0.2910	0.2939	0.2967	0.2995	0.3023	0.3051	0.3078	0.3106	0.3133
0.9	0.3159	0.3186	0.3212	0.3238	0.3264	0.3289	0.3315	0.3340	0.3365	0.3389
1.0	0.3413	0.3438	0.3461	0.3485	0.3508	0.3531	0.3554	0.3577	0.3599	0.3621
1.1	0.3643	0.3665	0.3686	0.3708	0.3729	0.3749	0.3770	0.3790	0.3810	0.3830
1.2	0.3849	0.3869	0.3888	0.3907	0.3925	0.3944	0.3962	0.3980	0.3997	0.4015
1.3	0.4032	0.4049	0.4066	0.4082	0.4099	0.4115	0.4131	0.4147	0.4162	0.4177
1.4	0.4192	0.4207	0.4222	0.4236	0.4251	0.4265	0.4279	0.4292	0.4306	0.4319
1.5	0.4332	0.4345	0.4357	0.4370	0.4382	0.4394	0.4406	0.4418	0.4429	0.4441
1.6	0.4452	0.4463	0.4474	0.4484	0.4495	0.4505	0.4515	0.4525	0.4535	0.4545
1.7	0.4554	0.4564	0.4573	0.4582	0.4591	0.4599	0.4608	0.4616	0.4625	0.4633
1.8	0.4641	0.4649	0.4656	0.4664	0.4671	0.4678	0.4686	0.4693	0.4699	0.4706
1.9	0.4713	0.4719	0.4726	0.4732	0.4738	0.4744	0.4750	0.4756	0.4761	0.4767
2.0	0.4772	0.4778	0.4783	0.4788	0.4793	0.4798	0.4803	0.4808	0.4812	0.4817
2.1	0.4821	0.4826	0.4830	0.4834	0.4838	0.4842	0.4846	0.4850	0.4854	0.4857
2.2	0.4861	0.4864	0.4868	0.4871	0.4875	0.4878	0.4881	0.4884	0.4887	0.4890
2.3	0.4893	0.4896	0.4898	0.4901	0.4904	0.4906	0.4909	0.4911	0.4913	0.4916
2.4	0.4918	0.4920	0.4922	0.4925	0.4927	0.4929	0.4931	0.4932	0.4934	0.4936
2.5	0.4938	0.4940	0.4941	0.4943	0.4945	0.4946	0.4948	0.4949	0.4951	0.4952
2.6	0.4953	0.4955	0.4956	0.4957	0.4959	0.4960	0.4961	0.4962	0.4963	0.4964
2.7	0.4965	0.4966	0.4967	0.4968	0.4969	0.4970	0.4971	0.4972	0.4973	0.4974
2.8	0.4974	0.4975	0.4976	0.4977	0.4977	0.4978	0.4979	0.4979	0.4980	0.4981
2.9	0.4981	0.4982	0.4982	0.4983	0.4984	0.4984	0.4985	0.4985	0.4986	0.4986
3.0	0.4987	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990

Control Chart Factors

n	d2	A2	d3	D3	D4
2	1.128	1.880	0.853	0.000	3.267
3	1.693	1.023	0.888	0.000	2.575
4	2.059	0.729	0.880	0.000	2.282
5	2.326	0.577	0.864	0.000	2.114
6	2.534	0.483	0.848	0.000	2.004
7	2.704	0.419	0.833	0.076	1.924
8	2.847	0.373	0.820	0.136	1.864
9	2.970	0.337	0.808	0.184	1.816
10	3.078	0.308	0.797	0.223	1.777
11	3.173	0.285	0.787	0.256	1.744
12	3.258	0.266	0.778	0.283	1.717
13	3.336	0.249	0.770	0.307	1.693
14	3.407	0.235	0.763	0.328	1.672
15	3.472	0.223	0.756	0.347	1.653
16	3.532	0.212	0.750	0.363	1.637
17	3.588	0.203	0.744	0.378	1.622
18	3.640	0.194	0.739	0.391	1.609
19	3.689	0.187	0.733	0.404	1.596
20	3.735	0.180	0.729	0.415	1.585
21	3.778	0.173	0.724	0.425	1.575
22	3.819	0.167	0.720	0.435	1.565
23	3.858	0.162	0.716	0.443	1.557
24	3.895	0.157	0.712	0.452	1.548
25	3.931	0.153	0.708	0.459	1.541